Multiple Endpoints in Clinical Trials

Guidance for Industry

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U.S. Department of Health and Human Services Food and Drug Administration Center for Drug Evaluation and Research (CDER) Center for Biologics Evaluation and Research (CBER)

> [January 2017] Clinical/Medical

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Multiple Endpoints in Clinical Trials Guidance for Industry¹

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I. INTRODUCTION

16 17 This guidance provides sponsors and review staff with the Agency's thinking about the problems 18 posed by multiple endpoints in the analysis and interpretation of study results and how these 19 problems can be managed in clinical trials for human drugs, including drugs subject to licensing 20 as biological products. Most clinical trials performed in drug development contain multiple 21 endpoints to assess the effects of the drug and to document the ability of the drug to favorably 22 affect one or more disease characteristics. As the number of endpoints analyzed in a single trial 23 increases, the likelihood of making false conclusions about a drug's effects with respect to one or 24 more of those endpoints becomes a concern if there is not appropriate adjustment for 25 multiplicity. The purpose of this guidance is to describe various strategies for grouping and ordering endpoints for analysis and applying some well-recognized statistical methods for 26 27 managing multiplicity within a study in order to control the chance of making erroneous 28 conclusions about a drug's effects. Basing a conclusion on an analysis where the risk of false 29 conclusions has not been appropriately controlled can lead to false or misleading representations 30 regarding a drug's effects.

31

FDA's guidance for industry *E9 Statistical Principles for Clinical Trials* (International Council
on Harmonisation E9 guidance, or "ICH E9")² is a broad ranging guidance that includes
discussion of multiple endpoints. This guidance on multiple endpoints in clinical trials for
human drugs provides greater detail on the topic. The issuance of this guidance represents
partial fulfillment of an FDA commitment under the Food and Drug Administration
Amendments Act (FDAAA) of 2007.

³⁸

¹ This guidance has been prepared by the Office of Biostatistics in the Office of Translational Sciences in the Center for Drug Evaluation and Research at the Food and Drug Administration.

² The ICH E9 guidance is available on the FDA Drugs Web page under ICH – Efficacy. We update guidances periodically. To make sure you have the most recent version of a guidance, check the FDA Drugs Web page at <u>http://www.fda.gov/Drugs/GuidanceComplianceRegulatoryInformation/Guidances/default.htm</u>.

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39 In general, FDA's guidance documents do not establish legally enforceable responsibilities.

40 Instead, guidances describe the Agency's current thinking on a topic and should be viewed only

41 as recommendations, unless specific regulatory or statutory requirements are cited. The use of

the word *should* in Agency guidances means that something is suggested or recommended, butnot required.

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46 II. BACKGROUND AND SCOPE

Failure to account for multiplicity when there are several clinical endpoints evaluated in a study
can lead to false conclusions regarding the effects of the drug. The regulatory concern regarding
multiplicity arises principally in the evaluation of clinical trials intended to demonstrate
effectiveness and support drug approval; however, this issue is important throughout the drug
development process.

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54 55

A. Introduction to Study Endpoints

56 Efficacy endpoints are measures intended to reflect the effects of a drug. They include

57 assessments of clinical events (e.g., mortality, stroke, pulmonary exacerbation, venous

thromboembolism), patient symptoms (e.g., pain, dyspnea, depression), measures of function

59 (e.g., ability to walk or exercise), or surrogates of these events or symptoms.

60

61 Because most diseases have more than one consequence, many trials are designed to examine the

62 effect of a drug on more than one endpoint. In some cases, efficacy cannot be adequately

63 established on the basis of a single endpoint. In other cases, an effect on any of several

64 endpoints could be sufficient to support approval of a marketing application. When the rate of

65 occurrence of a single event is expected to be low, it is common to combine several events (e.g.,

66 cardiovascular death, heart attack, and stroke) in a "composite event endpoint" where the

67 occurrence of any of the events would constitute an "endpoint event."

68

When there are many endpoints prespecified in a clinical trial, they are usually classified intothree families: primary, secondary, and exploratory.

The set of primary endpoints consists of the outcome or outcomes (based on the drug's expected effects) that establish the effectiveness, and/or safety features, of the drug in order to support regulatory action. When there is more than one primary endpoint and success on any one alone could be considered sufficient to demonstrate the drug's effectiveness, the rate of falsely concluding the drug is effective is increased due to multiple comparisons (see section II.E).

Secondary endpoints may be selected to demonstrate additional effects after success on the primary endpoint. For instance, a drug may demonstrate effectiveness on the primary endpoint of survival, after which the data regarding an effect on a secondary endpoint, such as functional status, would be tested. Secondary endpoints may also provide evidence that a particular mechanism underlies a demonstrated clinical effect (e.g., a drug for osteoporosis with fractures as the primary endpoint, and improved bone density as a secondary endpoint).

• All other endpoints are referred to as exploratory in this document (see section III.A).

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85 Endpoints are frequently ordered by clinical importance, with the most important being 86 designated as primary (e.g., mortality or irreversible morbidity). This is not always done, however, for a variety of reasons. The most common reasons not to order endpoints by clinical 87 88 importance are if there are likely to be too few of the more clinically important endpoint events 89 to provide adequate power for the study, or if the effect on a clinically less important endpoint is 90 expected to be larger. In these cases, endpoints are often ordered by the likelihood of 91 demonstrating an effect. For example, time-to-disease progression is often selected as the 92 primary endpoint in oncology trials even though survival is almost always the most important 93 endpoint; the reasons being that an effect on disease progression may be more readily 94 demonstrable, may be detected earlier, and often has a larger effect size because the observed 95 effect on survival can be diluted by subsequent treatment post-progression. Section III.A 96 includes further discussion of the primary and secondary endpoint families. The determination 97 of which endpoints are primary, secondary, or exploratory, regardless of the reasons for the 98 determination, should always be made prospectively (see ICH E9). 99 100 Although this guidance focuses on endpoints intended to demonstrate effectiveness, a study that

101 is designed specifically to assess safety outcomes may also have both primary and secondary

endpoints, which would then be subject to the same multiplicity considerations described in this
 guidance.

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- 105 106

B. Demonstrating the Study Objective of Effectiveness

107 A conclusion that a study has demonstrated an effect of a drug is critical to meeting the legal 108 standard for substantial evidence of effectiveness required to support approval of a new drug 109 (i.e., "... adequate and well-controlled investigations...on the basis of which it could fairly and 110 responsibly be concluded...that the drug will have the effect it purports...to have...") (section 505(d) of the FD&C Act).³ FDA regulations further establish that to be adequate and well 111 112 controlled, a clinical study of a drug must include, among other things, "an analysis of the results of the study adequate to assess the effects of the drug," a requirement that furthers the "purpose 113 of conducting clinical investigations of a drug" which is "to distinguish the effect of a drug from 114 other influences, such as spontaneous change in the course of the disease, placebo effect, or 115 biased observation."⁴ The clinical trial community has accepted an approach that finds a 116 117 treatment effect to be established when a determination is made that the apparent treatment effect 118 observed in a clinical trial is not likely to have occurred by chance. This is generally 119 accomplished by placing a limit on the probability that the finding is the result of chance. 120

³ Similarly, biological products are licensed based on a demonstration of safety, purity and potency (section 351(a)(2)(C) of the Public Health Service Act, 42 USC 262(a)(2)(C)). Potency has long been interpreted to include effectiveness (21 CFR 600.3(s)). In 1972, FDA initiated a review of the safety and effectiveness of all previously licensed biologics. The Agency stated then that proof of effectiveness would consist of controlled clinical investigations as defined in the provision for adequate and well-controlled studies for new drugs (21 CFR 314.126), unless waived as not applicable to the biological product or essential to the validity of the study when an alternative method is adequate to substantiate effectiveness." (37 FR 16681, August 18, 1972).

⁴ See 21 CFR 314.126(b)(7), 314.126(a).

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121 The statistical approach commonly used to address the certainty/uncertainty in the assessment of

- 122 a treatment effect on a chosen clinical endpoint is based on the *test of hypothesis*. This approach
- begins with stating the relevant hypotheses for each endpoint. In the simplest situation, two
- 124 mutually exclusive hypotheses are specified for each endpoint in advance of conducting a
- 125 clinical trial:
- One hypothesis, the *null hypothesis*, states that there is no treatment effect on the chosen clinical endpoint. The treatment effect is represented by a parameter, for example, T-C, the difference between the test group's average outcome measure (T) and that of the control group (C), or T/C, the ratio of response rates for the two groups. The null hypothesis is represented by the equation T-C = 0 or T/C = 1, stating that the true difference between the outcomes for the test group and the control group is zero or the risk ratio is 1 (i.e., there is no treatment effect).
- The other hypothesis is called the *alternative hypothesis* and posits that there is at least some treatment effect of the test drug, usually represented as T-C > 0 (or T/C > 1) for the alternative of interest (a beneficial effect of the drug).
- 136

137 The *test of hypothesis* determines whether (1) the trial results are consistent with the null

hypothesis of no treatment effect or (2) the favorable result of the trial is so unlikely to have been obtained if the null hypothesis were true that the null hypothesis can be rejected and the

alternative hypothesis, that there is a treatment effect, accepted.

141

142 Sometimes (e.g., in some vaccine trials), demonstration of an effect of at least some minimum 143 size is considered essential for approval of a drug. In this case the null hypothesis might be 144 modified to $T-C \le m$ or $T/C \le r$, where *m* or *r* is the smallest effect that could be accepted. Such 145 modifications of the null hypothesis can have an impact on the sample size of a trial.

146 147

C. Type I Error

148 149 The rejection of the null hypothesis supports the study conclusion that there is a difference 150 between treatment groups but does not constitute absolute proof that the null hypothesis is false. 151 There is always some possibility of mistakenly rejecting the null hypothesis when it is, in fact, 152 true. Such an erroneous conclusion is called a Type I error. Null hypothesis rejection is based 153 on a determination that the probability of observing a result at least as extreme as the result of the 154 study assuming the null hypothesis is true (the p-value) is sufficiently low. The probability of 155 concluding that there was a difference between treatment groups due to the drug when, in fact, 156 there was none, is called the Type I error probability or rate, denoted as alpha (α). 157 158 Type I error probabilities can apply to two-sided hypothesis tests, in which case they refer to the 159 probability of concluding that there is a difference (beneficial or harmful) between the drug and 160 control when there is no difference. Type I error probabilities can also apply to one-sided 161 hypothesis tests, in which case they refer to the probability of concluding specifically that there 162 is a *beneficial difference* due to the drug when there is not. The most widely-used values for 163 alpha are 0.05 for two-sided tests and 0.025 for one-sided tests. In the case of one-sided tests, an 164 alpha of 0.025 means that the probability of falsely concluding a beneficial effect of the drug

- when none exists is no more than 2.5 percent, or 1 chance in 40 (represented as $p \le 0.025$). In
- 166 the case of two-sided tests, an alpha of 0.05 means that the probability of falsely concluding that

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167 the drug differs from the control in either direction (benefit or harm) when no difference exists is 168 no more than 5 percent, or 1 chance in 20 (represented as p < 0.05). Use of a two-sided test with 169 an alpha of 0.05 generally also ensures that the probability of falsely concluding *benefit* when 170 there is none is no more than approximately 2.5 percent (1 chance in 40). Use of either test 171 therefore provides strong assurance against the possibility of a false-positive result (i.e., no more 172 than 1 chance in 40) and a sound basis for regulatory decision-making, especially when 173 substantiated by another study or other confirmatory evidence.⁵ 174 175 For simplicity, this guidance discusses statistical testing of two-sided hypotheses at the 5 percent 176 level, with the understanding that the one-sided alternative hypothesis of a beneficial drug effect 177 is our focus, and the chance of a false positive conclusion is our primary concern. In most cases, 178 sponsors can perform either two-sided or one-sided tests of hypothesis, at their discretion. 179 180 This discussion is focused on the study's final analysis. If interim analyses occur during a study, 181 there should be a prospective plan to ensure that these additional analyses do not increase the 182 chances of a false positive conclusion. When multiple endpoints are examined at an interim 183 analysis, the appropriate adjustments can become complex; discussion of this issue is outside the 184 scope of this guidance. 185 186 FDA's concern for controlling the Type I error probability is to minimize the chances of a false 187 favorable conclusion for any of the primary or secondary endpoints, regardless of which and how 188 many endpoints in the study have no effect (called strong control of the Type I error probability). 189 Determining if strong control is achieved can be complicated when more than one endpoint is 190 under consideration, any one of which could support a conclusion that the treatment has a 191 beneficial effect. When there is more than one study endpoint, care must be taken to ensure that 192 the evaluation of multiple hypotheses does not lead to inflation of the study's overall Type I error 193 probability, called the study-wise Type I error probability, which is the chance of a false positive 194 conclusion on any planned endpoint analysis. 195 196 The discussion of specific statistical methods for managing multiplicity in section IV illustrates 197 that when some of the null hypotheses should be rejected but others should not be rejected, the 198 control of the Type I error probability can become complex. The challenge that arises from 199 testing multiple hypotheses associated with multiple endpoints in a study is to ensure that there is 200 a proper accounting for all of the possible ways the endpoints of the study could produce false 201 positive conclusions (see section II.E). 202 203 An essential element of Type I error rate control is the prospective specification of: 204 all endpoints that will be tested and • 205 all data analyses that will be performed to test hypotheses about the prespecified • 206 endpoints. 207 For a multiple endpoints study, the analysis plan should describe how (or ways to determine 208 how) the endpoints are tested, including the order of testing and the alpha level applied to each 209

specific test.

⁵ See the FDA guidance for industry *Providing Clinical Evidence of Effectiveness for Human Drug and Biological* Products, available on the FDA Drugs guidance Web page under Clinical/Medical.

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D. **Relationship Between the Observed and True Treatment Effects**

213 The statistical analysis associated with a hypothesis test produces three primary measures of 214 interest:

- a point estimate,
 - a confidence interval, and
- 217 a p-value. •

218 The effect of the treatment is typically presented as a point estimate (the observed T-C

219 difference) that represents the most likely true effect. The confidence interval is usually two-220 sided and illustrates the range of true treatment effect values consistent with the data observed in 221 the trial.

222

223 In addition to the point estimate of the treatment effect, it is important to consider the width of 224 the confidence interval. The confidence interval provides a measure of the precision of the

225 estimate of the treatment effect. The narrower the confidence interval, and the further away its

226 lower bound is from the null hypothesis of no treatment effect (T-C = 0 or T/C = 1), the more

227 confident we are of both the magnitude and existence of the treatment effect. Generally, the

228 farther the lower bound of the confidence interval is from zero (or 1), the more persuasive

229 (smaller) the p-value is and the lower the likelihood that the effectiveness finding was a chance occurrence.

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234

232 There is usually a relationship between the test of a hypothesis and the confidence interval; each 233 focuses on related but not identical questions:

- The test of a hypothesis focuses on whether or not there is an effect. •
- 235 The confidence interval focuses on the magnitude of the effect and the precision with • 236 which we know it.

237 The emphasis of this guidance is not on the confidence interval, but rather on the test of a 238 hypothesis, where the issue is whether a treatment effect on a particular endpoint exists at all. 239 Although confidence intervals are also critical to the interpretation of an effect when one exists, 240 determining the confidence interval with some of the statistical methods for managing 241 multiplicity described in section IV is complex. The primary goal of this guidance is to provide 242 recommendations for designing studies that control the chances of erroneously concluding that a 243 treatment is effective with respect to a particular endpoint. In some areas, however, confidence 244 intervals are used to test hypotheses of the type described at the end of section II.B (e.g., $T-C \leq$

- 245 m). In these situations, it is critical to ensure that the confidence intervals appropriately reflect 246 multiplicity of hypothesis tests.
- 247

E.

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Multiplicity

250 As described in section I.A, clinical trials often include more than one endpoint as an indicator of

251 effectiveness. When a trial is designed so that more than one study endpoint or comparison (of 252 treatment to control) could lead to a conclusion that effectiveness was established, testing each

253 endpoint separately at $\alpha = 0.05$ will inflate the Type I error rate and overstate the statistical

254 significance. The inflation of the Type I error rate can be quite substantial if there are many

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255 comparisons. Because this form of Type I error rate inflation is the result of multiple 256 comparisons, it is termed a multiplicity problem.

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258 In a clinical trial with a single endpoint tested at $\alpha = 0.05$, the probability of finding a difference 259 between the treatment group and a control group by chance alone is at most 0.05 (a 5 percent 260 chance). By contrast, if there are two independent endpoints, each tested at $\alpha = 0.05$, and if 261 success on either endpoint by itself would lead to a conclusion of a drug effect, there is a 262 multiplicity problem. For each endpoint individually, there is at most a 5 percent chance of 263 finding a treatment effect when there is no effect on the endpoint, and the chance of erroneously 264 finding a treatment effect on at least one of the endpoints (a false positive finding) is about 10 265 percent. More precisely, when the endpoints are independent, there is a 95 percent chance of 266 correctly failing to detect an effect for each endpoint if there is no true effect for either endpoint. 267 The chance of correctly failing to detect an effect on both endpoints together is thus 0.95 * 0.95, 268 which equals 0.9025, and so the probability of falsely detecting an effect on at least one endpoint 269 is 1 - 0.9025, which equals 0.0975. Without correction, the chance of making a Type I error for 270 the study as a whole would be 0.1 and the study-wise Type I error rate is therefore not 271 adequately controlled. The problem is exacerbated when more than two endpoints are 272 considered. For three endpoints, the Type I error rate is 1 - (.95 * .95 * .95), which is about 14

273 percent. For ten endpoints, the Type I error rate is about 40 percent.

274

275 Even when a single outcome variable is being assessed, if the approach to evaluating the study 276 data is to analyze multiple facets of that outcome (e.g., multiple dose groups, multiple time

277 points, or multiple patient subgroups based on demographic or other characteristics) and regard

- 278 the study as positive (i.e., conclude that the drug has been shown to produce a beneficial effect)
- 279 if any one analysis is positive, the multiplicity of analyses causes inflation of the Type I error
- 280 rate, thus increasing the probability of reaching a false conclusion about the effects of the drug.
- 281 Similarly, application of more than one analytic approach to one endpoint introduces multiplicity
- 282 by providing additional ways for the trial to be successful (to "win"). Examples include
- 283 conducting both unadjusted and covariate-adjusted analyses, use of different analysis populations
- 284 (intent-to-treat, completers, per protocol), use of different endpoint assessments (by investigator
- 285 vs. a central endpoint assessment committee), and many others. By inflating Type I error,
- 286 multiplicity produces uncertainty in interpretation of the study results such that the strength of a 287 finding becomes unclear, and conclusions about whether effectiveness has been demonstrated in
- 288 the study become unreliable. There are various approaches that can be planned prospectively
- 289 and applied to maintain the Type I error rate at 5 percent. Among these are adjustments to the
- 290 alpha level for determining that an individual endpoint test is positive, structuring the order in 291 which the endpoints are tested, and others. These approaches are discussed in detail in section IV.
- 292
- 293

294 An important principle for controlling multiplicity is to prospectively specify all planned 295 endpoints, time points, analysis populations, and analyses. Once these factors are specified,

296 appropriate adjustments for multiple endpoints and analyses can be planned and applied, as

- 297 needed. Changes in the analytic plan to perform additional analyses, however, can reintroduce a
- 298 multiplicity problem that can negatively impact the ability to interpret the study's results unless
- 299 these changes are made prior to data analysis and appropriate multiplicity adjustments are
- 300 performed. In the past, it was not uncommon, after the study was unblinded and analyzed, to see

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301 a variety of post hoc adjustments of design features (e.g., endpoints, analyses), usually plausible 302 on their face, to attempt to elicit a positive study result from a failed study — a practice 303 sometimes referred to as data-dredging. Although post hoc analyses of trials that fail on their 304 prospectively specified endpoints may be useful for generating hypotheses for future testing, 305 they do not yield definitive results. The results of such analyses can be biased because the 306 choice of analyses can be influenced by a desire for success. The results also represent a 307 multiplicity problem because there is no way to know how many different analyses were 308 performed and there is no credible way to correct for the multiplicity of statistical analyses and 309 control the Type I error rate. Consequently, post hoc analyses by themselves cannot establish 310 effectiveness. Also, additional endpoints that have not been pre-specified or evaluated with 311 adjustment for multiplicity when required cannot, in general, be used to demonstrate an effect of 312 the drug, even in successful studies.

313

314 The multiplicity problem is also an issue in safety evaluations of controlled trials. With the

315 exception of trials designed specifically to evaluate a particular safety outcome of interest, in

- 316 typical safety assessments, there are often (1) no prior hypotheses, (2) many plausible analyses,
- 317 (3) numerous safety findings that would be of concern, and (4) interest in both individual large
- 318 studies and pooled study results. Moreover, it is difficult to discern what the analytic plan was
- and how it might have changed. There is no easy remedy for these issues, beyond recognition of
- the problems and a search for additional support that a finding is not a matter of chance. For
- 321 example, it is more credible that there is a causal relationship between an observed adverse event 322 and the drug, if the findings are consistent across studies; are predicted on the basis of
- recognized class effects, mechanism of drug action, or nonclinical studies; or are related to dose
- 324 or exposure. The multiplicity problems for these types of safety analyses are outside the scope 325 of this guidance.
- 326

The focus of this guidance is control of the Type I error rate for the planned primary and

328 secondary endpoints of a clinical trial so that the major findings are well supported and the 329 effects of the drug have been demonstrated. Once a trial is successful (demonstrates

effectiveness or "wins" on the primary endpoint(s)), there are many other attributes of a drug's

- 331 effects that may be described. Analyses that describe these other attributes of a drug can be
- informative and are often included in physician labeling.⁶ Examples include: the time course of
- 333 treatment effects;⁷ the full distribution of responses amongst participants;⁸ treatment effects on
- the components of a composite endpoint;⁹ and treatment effects amongst subgroups.¹⁰

⁷See, e.g., labeling for Pulmicort Flexhaler™ (budesonide) at http://www.accessdata.fda.gov/drugsatfda_docs/label/2010/021949s006lbl.pdf.

⁸ See, e.g., labeling for tetrabenazine at http://www.accessdata.fda.gov/drugsatfda_docs/label/2015/206129Orig1s000lbl.pdf.

⁹ See, e.g., labeling for COZAAR® (losartan potassium) at http://www.accessdata.fda.gov/drugsatfda_docs/label/2014/020386s061lbl.pdf.

⁶ FDA guidance for industry *Clinical Studies Section of Labeling for Human Prescription Drug and Biological Products — Content and Format*, available on the FDA Drugs guidance Web page under Labeling.

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335 Nevertheless, it is important to understand that these descriptions with respect to additional 336 attributes are not demonstrated additional effects of a drug unless the analyses were prespecified, 337 and appropriate multiplicity adjustments were applied. Therefore, presenting p-values from 338 descriptive analyses (that is, from analyses that were not prespecified and for which appropriate 339 multiplicity adjustments were not applied) is inappropriate because doing so would imply a 340 statistically rigorous conclusion and convey a level of certainty about the effects that is not 341 supported by that trial. Descriptive analyses are not the subject of this guidance and are not 342 addressed in detail. 343 344 In the following sections, the issues of multiple endpoints and methods to address them are

344 In the following sections, the issues of multiple endpoints and methods to address them are 345 illustrated with examples of different study endpoints. Both the issues and methods that apply to 346 multiple endpoints also apply to other sources of multiplicity, including multiple doses, time 347 points, or study population subgroups.

- 349 III. MULTIPLE ENDPOINTS: GENERAL PRINCIPLES
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351 352

A. The Hierarchy of Families of Endpoints

353 Endpoints in adequate and well-controlled drug trials are usually grouped hierarchically, often 354 according to their clinical importance, but also taking into consideration the expected frequency 355 of the endpoint events and anticipated drug effects. The critical determination for grouping 356 endpoints is whether they are intended to establish effectiveness to support approval or intended 357 to demonstrate additional meaningful effects. Endpoints essential to establish effectiveness for 358 approval are called *primary endpoints*. Secondary endpoints may be used to support the primary 359 endpoint(s) and/or demonstrate additional effects. The third category in the hierarchy includes 360 all other endpoints, which are referred to as exploratory. *Exploratory endpoints* may include 361 clinically important events that are expected to occur too infrequently to show a treatment effect 362 or endpoints that for other reasons are thought to be less likely to show an effect but are included to explore new hypotheses. Each category in the hierarchy may contain a single endpoint or a 363 364 family of endpoints.

- 365
- 366 367

1. Primary Endpoint Family

The endpoint(s) that will be the basis for concluding that the study met its objective (i.e., the study "wins") is designated the primary endpoint or primary endpoint family. When there is a single pre-specified primary endpoint, there are no multiple endpoint-related multiplicity issues in the determination that the study achieved its objective; however, there could still be multiplicity issues for demonstration of effects on secondary endpoints.

373

Multiple primary endpoints occur in three ways, further described in section III.C. The first is when there are multiple primary endpoints corresponding to multiple chances to "win," and in

¹⁰ See, e.g., labeling for BRILINTA® (ticagrelor) at http://www.accessdata.fda.gov/drugsatfda_docs/label/2015/022433s017lbl.pdf.

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376 this case, failure to adjust for multiplicity can lead to a false conclusion that the drug is effective. 377 The second is where determination of effectiveness depends on success on all of two or more 378 primary endpoints. In this setting, there are no multiple endpoint-related multiplicity issues, and 379 therefore, no concern with Type I error rate inflation, but there is a concern with Type II error 380 rate inflation (See Section III.B). In the third, critical aspects of effectiveness can be combined 381 into a single primary composite (or other multicomponent) endpoint, thereby avoiding multiple 382 endpoint-related multiplicity issues. For example, in many cardiovascular studies it is usual to 383 combine several endpoints (e.g., cardiovascular death, heart attack, and stroke) into a single 384 composite endpoint that is primary and to consider death a secondary endpoint (section III.A.2). 385 A comprehensive examination of the drug's effects earlier in development might aid in the 386 selection of a sensitive and informative measure of the drug's effect and allow use of a single 387 primary endpoint for the confirmatory trial.

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2. Secondary Endpoint Family

391 The collection of all secondary endpoints is called the secondary endpoint family. Secondary 392 endpoints are those that may provide supportive information about a drug's effect on the primary 393 endpoint or demonstrate additional effects on the disease or condition. Secondary endpoints 394 might include a pharmacodynamic effect that would not be considered an acceptable primary 395 efficacy endpoint but is closely related to the primary endpoint, (e.g., an effect consistent with 396 the drug's purported mechanism of action). A secondary endpoint could be a clinical effect 397 related to the primary endpoint that extends the understanding of that effect (e.g., an effect on 398 survival when a cardiovascular drug has shown an effect on the primary endpoint of heart 399 failure-related hospitalizations) or provide evidence of a clinical benefit distinct from the effect 400 shown by the primary endpoint (e.g., a disability endpoint in a multiple sclerosis treatment trial 401 in which relapse rate is the primary endpoint). In all cases, when an effect on the primary 402 endpoint is shown, the secondary endpoints can be examined and may contribute important 403 supportive information about a drug's effectiveness.

404

405 Positive results on the secondary endpoints can be interpreted *only* if there is first a
406 demonstration of a treatment effect on the primary endpoint family. The Type I error rate should

407 be controlled for the entire trial, defined in section II.C as strong control. This includes

408 controlling the Type I error rate within and between the primary and secondary endpoint

409 families. Moreover, the Type I error rate should be controlled for any preplanned analysis of

410 pooled results across studies; pooled analyses are rarely conducted for the planned primary

411 endpoint, but are sometimes used to assess lower frequency events, such as cardiovascular

412 deaths, where the individual trials used a composite endpoint, such as death plus hospitalization.

413 Statistical testing strategies to accomplish this are discussed in section IV. Control of the Type I

414 error rate for all endpoints depends upon the prospective designation of all primary and

415 secondary endpoints. Generally, the endpoints and analytical plan should be provided at the time

416 the trial protocol is finalized. The statistical analysis plan should not be changed after 417 unmasking of treatment assignments, including unmasking for any interim analyses.

418

419 Because study sample size is often determined based only on the amount of information needed

420 to adequately assess the primary hypothesis, many studies lack sufficient power to demonstrate

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421 effects on secondary endpoints. If success on the secondary endpoints is important, the

422 secondary endpoints should be considered when determining study design (e.g., sample size).

423

424 An example of a secondary endpoint used to further characterize the drug's effect is a

- 425 measurement of the primary outcome variable at 30 days in a trial whose primary endpoint is the
- 426 same outcome measured at 6 months. Another example is a secondary endpoint of the
- 427 percentage of patients whose symptoms are "very improved," when the primary endpoint is the
- 428 percentage of patients with any amount of improvement for the same symptoms. Adjustment for
- 429 multiplicity is necessary to demonstrate these additional effects.
- 430

431 It is recommended that the list of secondary endpoints be short, because the chance of

- 432 demonstrating an effect on any secondary endpoint after appropriate correction for multiplicity
- 433 becomes increasingly small as the number of endpoints increases. Endpoints intended to serve 434 the purpose of hypothesis generation should not be included in the secondary endpoint family.
- 434 the purpose of hypothesis generation should not be included in the secondary endpoint fami 435 These should be considered exploratory endpoints
- 435 These should be considered exploratory endpoints.
- 436

B. Type II Error Rate and Multiple Endpoints

437 438

439 One of the greatest concerns in the design of clinical trials intended to support drug approval is 440 inflation of the Type I error rate, because it can lead to an erroneous conclusion that a drug is 441 effective. FDA is also concerned with the risk of Type II error, which is failing to show an effect 442 of a drug where there actually is one. The intended level of risk of a Type II error is usually 443 denoted by the symbol beta (β). The study's likelihood of avoiding Type II error (1- β), if the 444 drug actually has the specified effect, is called study power. The desired power is an important 445 factor in determining the sample size.

446

447 The sample size of a study is generally chosen to provide a reasonably high power to show a 448 treatment effect if an effect of a specified size is in fact present. In addition to the treatment 449 effect, the optimal sample size of a study is influenced by the variability of the endpoint and the 450 alpha level specified for the test of hypothesis for that endpoint. Investigators should consider

451 these factors for all of the endpoints for which the study is intended to be well powered.

452

453 Many of the statistical adjustment methods to control the Type I error rate for multiplicity

discussed in section IV decrease study power because they lower the alpha level used for each ofthe individual endpoints' test of hypothesis, making it more difficult to achieve statistical

456 significance. Increasing the sample size appropriately can overcome this decrease in power. In

457 general, the greater the number of endpoints (analyses), the greater the statistical adjustment that

- 458 is needed and the greater the increase in the sample size of the trial necessary to maintain power
- 459 for all individual endpoints. This decrease in study power (i.e., increased Type II error rate)
- 460 from multiplicity is often a practical limiting factor in choosing the number of endpoints
- 461 designated for a trial as indicators of success without requiring an excessive sample size.
- 462

463 Some of the methods discussed in section IV to manage multiplicity are complex and may, for

464 example, call for the alpha level for any particular test of hypothesis to be determined by the

- 465 actual study endpoint results and the resulting sequence of hypothesis testing. In some cases,
- 466 sponsors may wish to have the study well powered for one or two secondary endpoints in

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467 addition to the primary endpoint family, further adding to the complexity. Determination of an 468 appropriate study sample size to ensure that the study is appropriately powered can be difficult in 469 these cases, and often will be dependent upon computer simulations rather than an analytic 470 formula, which can be used for simpler situations.

471

472 The use of two or more endpoints for which demonstration of an effect on each is needed to 473 support regulatory approval (called co-primary endpoints; see section III.C.1 below) increases 474 the Type II error rate and decreases study power. If, for example, the study sample size is 475 selected to provide 80 percent power to show success on each of two endpoints (i.e., Type II 476 error rate is 20 percent for each), and the endpoints are entirely independent, the power to show 477 success on both will be just 64 percent (0.8×0.8) : i.e., the likelihood of the study failing to 478 support a conclusion of a favorable drug effect when such an effect existed (the Type II error 479 rate) would be 36 percent. The study power could, of course, be restored by increasing the 480 sample size. Multiplicity and Type I error rate inflation are not a concern with co-primary 481 endpoints, as there is only one way to succeed.

482

483 The loss of power may not be so severe when the endpoints are correlated (i.e., not fully 484 independent). With positive correlation, there is an increased chance that a second endpoint will 485 demonstrate the treatment effect if one endpoint is successful, potentially increasing study power 486 well above the 64 percent estimate. Moreover, the individual endpoints usually do not all have 487 the same power-influencing characteristics because the effect size and variability estimates may 488 be different for the different endpoints. If the study is designed so that a test of the endpoint 489 upon which it is most difficult to demonstrate an effect has 80 percent power, the other endpoints 490 may have power in excess of 80 percent to show the expected effect. In that case, the overall 491 study power, even if the endpoints were fully independent, will also be higher than if all 492 endpoints were equally powered. Nonetheless, when considering use of co-primary endpoints in 493 a study, it should be recognized that use of more than two can markedly reduce study power.

- 494
- 495 496

C. **Types of Multiple Endpoints**

497 Multiple endpoints may be needed when determining that the drug confers a clinical benefit 498 depends on more than one disease aspect or outcome being affected. Multiple endpoints may 499 also be used when (1) there are several important aspects of a disease or several ways to assess 500 an important aspect, (2) there is no consensus about which one will best serve the study 501 purposes, and (3) an effect on any one will be sufficient as evidence of effectiveness to support 502 approval. In some cases, multiple aspects of a disease may appropriately be combined into a 503 single endpoint, but subsequent analysis of the components is generally important for an 504 adequate understanding of the drug's effect. These circumstances when multiple endpoints are 505 encountered are discussed below.

- 506
- 507 508

1.

When Demonstration of Treatment Effects on All of Two or More Distinct Endpoints Is Necessary to Establish Clinical Benefit (Co-Primary Endpoints)

509 510

The primary endpoint for determining that a drug is effective should encompass one or more of the important features of a disorder and should be clinically meaningful. There are two types of 511

512 circumstances when no single endpoint adequately serves this purpose.

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- 513
- 514 For some disorders, there are two or more different features that are so critically important to the
- 515 disease under study that a drug will not be considered effective without demonstration of a
- 516 treatment effect on all of these disease features. The term used in this guidance to describe this
- 517 circumstance of multiple primary endpoints is co-primary endpoints. Multiple primary endpoints
- 518 become co-primary endpoints when it is necessary to demonstrate an effect on each of the
- 519 endpoints to conclude that a drug is effective.
- 520

521 Therapies for the treatment of migraine headaches illustrate this circumstance. Although pain is

- 522 the most prominent feature, migraine headaches are also often characterized by the presence of 523 photophobia, phonophobia, and nausea, all of which are clinically important. Which of the three 524 is most clinically important varies among patients. A recent approach to studying treatments is
- 525 to consider a drug effective for migraines only if pain and an individually-specified most 526 bothersome second feature are both shown to be improved by the drug treatment.
- 527

528 A second kind of circumstance in which a demonstration of an effect on two endpoints is needed

529 is when there is a single identified critical feature of the disorder, but uncertainty as to whether

530 an effect on the endpoint alone is clinically meaningful. In these cases, two endpoints are often

531 used. One endpoint is specific for the disease feature intended to be affected by the drug but not

532 readily interpretable as to the clinical meaning, and the second endpoint is clinically interpretable

533 but may be less specific for the intended action of the test drug. A demonstration of 534 effectiveness is dependent upon both endpoints showing a drug effect. One endpoint ensures the

- 535 effect occurs on the core disease feature, and the other ensures that the effect is clinically
- 536 meaningful.
- 537

538 An example illustrating this second circumstance is development of drugs for treatment of the 539 symptoms of Alzheimer's disease. Drugs for Alzheimer's disease have generally been expected

540 to show an effect on both the defining feature of the disease, decreased cognitive function, and

541 on some measure of the clinical impact of that effect. Because there is no single endpoint able to

542 provide convincing evidence of both, co-primary endpoints are used. One primary endpoint is

- 543 the effect on a measure of cognition in Alzheimer's disease (e.g., the Alzheimer's Disease
- 544 Assessment Scale-Cognitive Component), and the second is the effect on a clinically
- 545 interpretable measure of function, such as a clinician's global assessment or an Activities of
- 546 Daily Living Assessment.
- 547

548 Trials of combination vaccines are another situation in which co-primary endpoints are

549 applicable. These vaccine trials are typically designed and powered for demonstration of a

550 successful outcome on effectiveness endpoints for each pathogen against which the vaccine is

- intended to provide protection. 551
- 552

553 As discussed in section II.E, multiplicity problems occur when there is more than one way to

554 determine that the study is a success. When using co-primary endpoints, however, there is only

555 one result that is considered a study success, namely, that all of the separate endpoints are

- 556 statistically significant. Therefore, testing all of the individual endpoints at the 0.05 level does
- 557 not cause inflation of the Type I error rate; rather, the impact of co-primary endpoint testing is to
- 558 increase the Type II error rate. The size of this increase will depend on the correlation of the co-

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559 primary endpoints. In general, unless clinically very important, the use of more than two co-560 primary endpoints should be carefully considered because of the loss of power. 561 562 There have been suggestions that the statistical testing criteria for each co-primary endpoint 563 could be relaxed (e.g., testing at an alpha of 0.06 or 0.07) to accommodate the loss in statistical 564 power arising from the need to show an effect on both endpoints. Relaxation of alpha is 565 generally not acceptable because doing so would undermine the assurance of an effect on each 566 disease aspect considered essential to showing that the drug is effective in support of approval. 567 568 When Demonstration of a Treatment Effect on at Least One of Several Primary 2. 569 Endpoints Is Sufficient 570 571 Many diseases have multiple sequelae, and an effect demonstrated on any one of these aspects 572 may support a conclusion of effectiveness. Selection of a single primary endpoint may be 573 difficult, however, if the aspect of a disease that will be responsive to the drug or the evaluation 574 method that will better detect a drug effect is not known a priori (at the time of trial design). In 575 this circumstance, a study might be designed such that success on any one of several endpoints 576 could support a conclusion of effectiveness. This creates a primary endpoint family. For 577 example, consider a drug for the treatment of burn wounds where it is not known whether the 578 drug will increase the rate of wound closure or reduce scarring, but the demonstration of either 579 effect alone would be considered to be clinically important. A study in this case might have both 580 wound closure rate and a scarring measure as separate primary endpoints. 581 582 This use of multiple endpoints creates a multiplicity problem because there are several ways for 583 the study to successfully demonstrate a treatment effect. Control of the Type I error rate for the 584 primary endpoint family is critical. A variety of approaches can be used to address this 585 multiplicity problem; section IV is devoted to describing and discussing some of these 586 approaches. 587 588 It should be noted that failure to demonstrate an effect on any one of the individual prespecified 589 primary endpoints does not preclude making valid conclusions with respect to the other 590 prespecified primary endpoints. From a regulatory perspective, the results for all of the 591 prespecified primary endpoints, both positive and negative, are considered in the overall 592 assessment of risks and benefits. 593 594 3. Composite Endpoints 595 596 There are some disorders for which more than one clinical outcome in a clinical trial is 597 important, and all outcomes are expected to be affected by the treatment. Rather than using each 598 as a separate primary endpoint (creating multiplicity) or selecting just one to be the primary 599 endpoint and designating the others as secondary endpoints, it may be appropriate to combine 600 those clinical outcomes into a single variable. This is called a "composite endpoint," where an 601 endpoint is defined as the occurrence or realization in a patient of any one of the specified 602 components. When the components correspond to distinct events, composite endpoints are often 603 assessed as the time to first occurrence of any one of the components, but in diseases where a 604 patient might have more than one event, it also may be possible to analyze total endpoint events

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605 (see section III.D.1). A single statistical test is performed on the composite endpoint; 606 consequently, no multiplicity problem occurs and no statistical adjustment is needed.

607

608 An important reason for using a composite endpoint is that the incidence rate of each of the

- 609 events may be too low to allow a study of reasonable size to have adequate power; the composite
- 610 endpoint can provide a substantially higher overall event rate that allows a study with a
- 611 reasonable sample size and study duration to have adequate power. Composite endpoints are
- 612 often used when the goal of treatment is to prevent or delay morbid, clinically important but
- 613 uncommon events (e.g., use of an anti-platelet drug in patients with coronary artery disease to 614 prevent myocardial infarction, stroke, and death).
- 615 616
- The choice of the components of a composite endpoint should be made carefully. Because the 617 occurrence of any one of the individual components is considered to be an endpoint event, each
- 618 of the components is of equal importance in the analysis of the composite. The treatment effect
- 619 on the composite rate can be interpreted as characterizing the overall clinical effect when the
- 620 individual events all have reasonably similar clinical importance. The effect on the composite
- 621 endpoint, however, will not be a reasonable indicator of the effect on all of the components or an
- 622 accurate description of the drug's benefit, if the clinical importance of different components is 623 substantially different and the drug effect is chiefly on the least important event. Furthermore, it 624 is possible that a component with greater importance may appear to be adversely affected by the
- 625 treatment, even if one or more event types of lesser importance are favorably affected, so that
- 626 although the overall outcome still has a favorable statistical result, doubt may arise about the
- 627 treatment's clinical value. In this case, although the overall statistical analysis indicates the 628 treatment is successful, careful examination of the data may call this conclusion into question.
- 629 For this reason, as well as for a greater depth of understanding of the treatment's effects,
- 630 analyses of the components of the composite endpoint are important (see section III.D) and can influence interpretation of the overall study results.
- 631 632
- 633 634

4. **Other Multi-Component Endpoints**

- A different type of multi-component endpoint is a within-patient combination of two or more 635 636 components. In this type of endpoint, an individual patient's evaluation is dependent upon 637 observation of all of the specified components in that patient. A single overall rating or status is 638 determined according to specified rules.
- 639
- 640 When the components are ordered categorical or continuous numeric scales, one way of forming 641
- an overall rating is to use the sum or average across the individual domain scores. Study 642 hypotheses are then tested by comparing the overall mean values between groups. Examples of
- 643
- this type are the Positive and Negative Syndrome Scale (PANSS) in schizophrenia research; the 644 Toronto Western Spasmodic Torticollis Rating Scale for evaluating cervical dystonia; the
- 645 Hamilton Rating Scale for Depression (HAM-D); the Brief Psychiatric Rating Scale; and many
- 646 patient-reported outcomes (PROs).
- 647
- 648 Alternatively, a multi-component endpoint may be a dichotomous (event) endpoint
- 649 corresponding to an individual patient achieving specified criteria on each of the multiple
- 650 components. This dichotomous form of a multi-component endpoint might be preferred over

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651 multiple independent endpoints in conditions where assuring individual patients have benefit on 652 all of several disease features is important. For example, the FDA guidance for industry 653 Considerations for Allogeneic Pancreatic Islet Cell Products recommends that the primary 654 endpoint in clinical trials of allogeneic pancreatic islet cells for Type 1 diabetes mellitus be a 655 composite in which patients are considered responders only if they meet two dichotomous 656 response criteria: normal range of HbA1c and elimination of hypoglycemia. In contrast, when 657 separate endpoints are analyzed as co-primary endpoints (i.e., all of the several identified disease 658 aspects are required to show an effect), the study provides evidence that the drug affects all of 659 the endpoints on a group-wise basis, but does not ensure an increase in the number of individual 660 patients for whom all endpoints are favorably affected. 661 662 More complex endpoint formulations may be appropriate when there are several different 663 features of a disease that are important, but not all features must be positively affected for a 664 patient to be regarded as receiving benefit. For example, a positive response for an individual patient might be defined as improvement in one or two specific required aspects of a disease 665 along with improvement in at least one, but not all, identified additional disease features, as in 666 667 the American College of Rheumatology (ACR) scoring system for rheumatoid arthritis. The 668 ACR20 criteria for defining a response to treatment are a 20 percent improvement in two specific 669 disease features (tender joints and swollen joints) and a 20 percent improvement in at least three 670 of five additional features (pain, acute phase reactants, global assessment by patient or physician, or disability). Generally, these types of endpoints are very disease-specific, and clinical research 671 672 on the particular disease and its manifestations guides the development of such defined, complex 673 combinations of assessments. These combinations, despite incorporating multiple different 674 features of the disease, provide a single primary endpoint for evaluating efficacy and do not raise multiplicity concerns.

- 675
- 676

677 The use of within-patient multi-component endpoints can be efficient if the treatment effects on 678 the different components are generally concordant. Study power can be adversely affected, 679 however, if there is limited correlation among the endpoints. Although multi-component 680 endpoints can provide some gains in efficiency compared to co-primary endpoints, the 681 appropriateness of a particular within-patient multi-component endpoint is generally determined 682 by clinical, rather than statistical, considerations. Formal statistical analyses of these 683 components without prespecification and adjustment for multiplicity, however, may lead to a 684 false conclusion about the effects of the drug with respect to each individual component, as 685 discussed in section III.D.

- 686
- 687

5. Clinically Critical Endpoints Too Infrequent for Use as a Primary Endpoint

688

689 For many serious diseases, there is an endpoint of such great clinical importance that it is 690 unreasonable not to collect and analyze the endpoint data; the usual example is mortality or 691 major morbidity events (e.g., stroke, fracture, pulmonary exacerbation). Even if relatively few of 692 these events are expected to occur in the trial, they may be included in a composite endpoint (see 693 section III.C.3) and also designated as a planned secondary endpoint to potentially support a 694 conclusion regarding effect on that separate clinical endpoint, if the effect of the drug on the 695 composite primary endpoint is demonstrated. There have been situations, however, where the 696 effect on the primary endpoint was not found to be statistically significant, but there did appear

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to be an effect on mortality or major morbidity. In the absence of a demonstrated treatment
effect on the primary endpoint, secondary endpoints cannot be assessed statistically, but the
suggestion of a favorable result on a major outcome such as mortality may be difficult to ignore.

One approach to avoid this situation would be to designate the mortality or morbidity endpoint as
another primary endpoint, and apply one of the statistical methods of section IV with unequal
splitting of the alpha. In this way, the endpoint can be validly tested, and should the effect be
large, it will provide evidence of efficacy. Depending upon how alpha is allocated, the increase
in sample size to maintain study power may only be modest.

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707 708

D. The Individual Components of Composite and Other Multi-Component Endpoints

709 710 711

1. Evaluating the Components of Composite Endpoints

712 For composite endpoints whose components correspond to events, an event is usually defined as 713 the first occurrence of any of the designated component events. Such composites can be 714 analyzed either with comparisons of proportions between study groups at the end of the study or 715 using time-to-event analyses. The time-to-event method of analysis is the more common method 716 when, within the study's timeframe of observation, the duration of being event-free is clinically 717 meaningful. Although there is an expectation that the drug will have a favorable effect on all the 718 components of a composite endpoint, that is not a certainty. Results for each component event 719 should therefore be individually examined and should always be included in study reports. 720 These analyses will not alter a conclusion about the statistical significance of the composite 721 primary endpoint and are considered descriptive analyses, not tests of hypotheses. If there is, 722 however, an interest in analyzing one or more of the components of a composite endpoint as 723 distinct hypotheses to demonstrate effects of the drug, the hypotheses should be part of the 724 prospectively specified statistical analysis plan that accounts for the multiplicity this analysis will 725 entail, as described above for mortality. 726

In analyzing the contribution of each component of a composite endpoint, there are two
approaches that differ in how patients who experience more than one of the event-types are
considered.

- One approach considers only the initial event in each patient. This method displays the incidence of each type of component event only when it was the first event for a patient.
 The sum of the first events across all categories will equal the total events for the composite endpoint.
- The other approach considers the events of each type in each patient. With this method,
 each of the components can also be treated as a distinct endpoint, irrespective of the order
 of occurrence, giving the numbers of patients who ever experienced an event of each
 type. In this case, each patient can be included in the event counts for more than one
 component, and the sum of events on all component types will be greater than the total
 number of composite events using only the first events.
- 740

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- An example to illustrate these approaches is the RENAAL trial, a study of the ability of losartan
- to delay development of diabetic nephropathy.¹¹ The primary endpoint was a composite
- endpoint of time to first occurrence of any one of three components: doubling of serum
- creatinine, progression to end-stage renal disease (ESRD), or death. Table 1 shows the crude
- incidence composite endpoint: there were 327 composite events in the losartan arm and 359 inthe placebo arm, which led to a statistically-significant difference in the time-to-event analysis.
- 747 The number of patients with an endpoint event at the end of study is tabulated in two ways.
- 748 First, the decomposition of the composite endpoint events shows only events that were the first
- event for a patient. Thus, in the losartan arm, 162 patients had doubling of serum creatinine as a
- 750 first event, 64 had ESRD, and 101 death. The total is 327, the same number as for the overall
- composite event, because only first events are counted. Table 1 includes the hazard ratio,
- confidence interval, and p-value for the primary composite endpoint. The confidence intervals
- and p-values are not given for the individual elements of the composite endpoint, because they
- were not designated as secondary endpoints and adequate control for multiplicity was not
- 755 specified to support their assessment.
- 756

757 Table 1. Decomposition of Endpoint Events in RENAAL*

Endpoint	Losartan	Placebo	Hazard ratio±	p-value
	(N=751)	(N=762)	(95% CI)	
Primary endpoint				
Doubling of serum				
creatinine, ESRD, or death	327	359	0.84 (0.72, 0.97)	0.022
Decomposition of the primary endpoint				
Doubling of serum	162	198	0.75	
Creatinine				
ESRD	64	65	0.93	
Death	101	96	0.98	
Any occurrence of individual components				
Doubling of serum	162	198	0.75 (0.61, 0.92)	
Creatinine				
ESRD	147	194	0.71 (0.57, 0.89)	
Death	158	155	1.02 (0.81, 1.27)	

758 *Excerpted from FDA/CDER/DBI Statistical Review at

759 (http://www.accessdata.fda.gov/drugsatfda_docs/nda/2002/20-386s028_Cozaar.cfm).

ESRD = end-stage renal disease; ±Hazard ratio from Cox proportional hazards time-to-event analysis.

761

The second analysis showing the results for any occurrence of individual components is quite

- 763 different from the first-event-only decomposition analysis. There are now more total events,
- because some patients experience more than one event type and these patients are included in
- both component-event counts. In this example, ESRD events at any time yield a hazard ratio of
- 766 0.71, which is markedly different from that obtained for ESRD in the first-event only analysis,

¹¹ RENAAL: The Reduction of Endpoints in NIDDM with the Angiotensin II Antagonist Losartan Study.

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767 0.93. Thus, the decomposition analysis limited to first events does not fully characterize the 768 effect of losartan on ESRD.

769

770 The analysis of any occurrence of an event type, however, can be complicated by the issue

771 known broadly in statistics as competing risks. This is the phenomenon wherein occurrence of

- 772 certain endpoints can make it impossible to observe other events in the same patient. For
- 773 example, in the RENAAL trial, patients whose first event was death could never be observed to
- 774 have doubling of serum creatinine. If one study group had higher early mortality, it could appear 775 to have a favorable profile with respect to other endpoint events simply because fewer patients
- 776 survived, diminishing the number of patients at risk for the other types of events.
- 777

778 Study design and patient management issues can also complicate interpretation of the

779 decomposition analyses. For example, in some trials, experiencing any endpoint event is cause

780 to remove a patient from study therapy and to initiate treatment with alternative agents, including

781 the possibility of receiving another treatment in the trial. Such a change in therapy obscures the

- 782 relationship between the initial study therapy and the occurrence of subsequent events, so that
- 783 only the analysis of first event will be useful. The complexities of interpretation of the 784
- decomposition analyses are important to consider when planning studies with a composite 785 endpoint.
- 786

788

787

2. Reporting and Interpreting the Individual Component Results of a Composite Endpoint

789 790 The different components of a composite endpoint are selected because they are all clinically 791 important; however, because each one is not necessarily equally affected by the drug, it is 792 relevant and important to examine the effects of the drug on the individual components as well as 793 on the overall endpoint. Presenting only data on the composite might imply meaningful 794 treatment effects on all of the individual components, when a composite effect may in fact be 795 established with little or no evidence of effect on some of the individual components. On the 796 other hand, showing the results of the analysis for each of the individual components may imply 797 an effect on an individual component when an appropriate statistical analysis would not support 798 that conclusion. Thus, it is important to present descriptive analyses of between-group 799 differences for the components in a way that does not overstate the conclusions.

800

801 It is common for one component of a composite endpoint to overly influence the treatment

802 effect, but even if that is not so, and all components contribute, the inclusion of a particular

803 component in a composite does not usually support an independent conclusion of efficacy on that

804 component. FDA's guidance for industry Clinical Studies Section of Labeling for Human

Prescription Drug and Biological Products — Content and Format¹² calls for presentation in 805

- 806 labeling of the components of a composite endpoint but without a statistical analysis of the
- 807 separate components unless the components were prespecified as separate endpoints and
- 808 assessed with a prospectively defined hypothesis and statistical analysis plan. In such a case, the 809 statistical analysis will usually consider all events of each type, not just first-occurring events (as
- 810

illustrated in Table 1 above). Only findings on prespecified endpoints that are statistically

¹² Available on the FDA Drugs Guidance Web page under Labeling.

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811 significant, with adjustment for multiplicity, are considered demonstrated effects of a drug. All 812 other findings are considered descriptive and would require further study to demonstrate that they are true effects of the drug. For example, a composite endpoint that includes mortality as a 813 814 component provides little information about effects on mortality if there are few deaths, and 815 presentations can make that clear by showing the actual numbers of deaths. Therefore, clear 816 presentation of the results of the components of a composite is essential to describe where the 817 drug's effect occurs. For example, the LIFE trial comparing losartan and atenolol in people with 818 hypertension showed a clear, statistically-significant advantage of losartan on the composite 819 endpoint of death, nonfatal myocardial infarction, or stroke, but this appeared to be related to an 820 effect on fatal and nonfatal stroke, with no advantage on the incidence of acute myocardial 821 infarction or cardiovascular death.¹³ 822 823 To demonstrate an effect on a specific component or components of a composite endpoint, the 824 component or components should be included prospectively as a secondary endpoint for the

component or components should be included prospectively as a secondary endpoint for the
study or possibly as an additional primary endpoint (see section III.C.5), with appropriate Type I
error rate control. If control of the Type I error rate is ensured with respect to the individual
component or components, in addition to control for the composite, a trial will be potentially
able to support conclusions regarding drug effects on the individual component or components as
well as the composite.

830 831

832

3. Evaluating and Reporting the Results on Other Multi-Component Endpoints

833 As with composite endpoints, understanding which components of a within-patient multi-834 component endpoint (e.g., symptom rating scale such as HAM-D) have contributed most to the 835 overall statistical significance could be important to correctly understanding the clinical effects 836 of the drug. Consequently, a descriptive analysis of the study results on the individual 837 components (or, in some cases, groups of similar components) may be considered but, as stated 838 previously, if undertaken, should be presented in a way that does not overstate the conclusions. 839 Unlike the composite endpoint used for outcome studies, where each component usually has 840 clear clinical importance (death, acute myocardial infarction, stroke, hospitalization), the clinical 841 importance of the components of these patient assessments may be less clear. Thus, for many of 842 these multi-component endpoints, the overall score is regarded as comprehensive and clinically 843 interpretable. The individual components of the scales, however, may not be independently 844 clinically interpretable. Although some rating scales have been developed with broad 845 multicomponent domains to allow the domains to be interpretable subsets of the overall scale, 846 the individual domain and subscale scores generally are not prespecified for hypothesis testing. 847 Prespecification of subscale scores with appropriate multiplicity control is required if it is thought to be important to demonstrate an effect of a drug on one or more of these subscale 848 849 scores in addition to the overall multi-component endpoint. 850

851 Analyses of specific component item(s) of a symptom rating scale as explicit endpoints in the

primary or secondary endpoint families may be reasonable, contingent on being clinically
 interpretable, in two cases:

¹³ LIFE: The Losartan Intervention For Endpoint reduction in hypertension study.

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(1) where earlier trials have suggested targeted efficacy of a drug on one or a small
number of specific symptoms, or
(2) where the specific symptom measured by the item is considered to be of substantial
inherent clinical importance.
An example of the first type is a novel agent for rheumatoid arthritis that was found in a
controlled phase 2 trial to be particularly effective in lessening patients' pain. In this example, a
sponsor might wish to test this hypothesis using a pain scale as a secondary endpoint in a trial
where improvement meeting ACR20 criteria, which include pain as a component, is the primary
endpoint. An example of the second type of component analysis might be found in trials of anti-
psychotic drugs, in which positive and negative symptoms are domains collected in the Positive
and Negative Syndrome Scale (PANSS) and often analyzed separately in addition to the overall
scale. Interpretation of analyses of any subscale domain, however, is dependent on that subscale
domain having been previously evaluated and determined to be valid as a stand-alone clinical
measure. As described above (see section III.C), control of the Type I error rate will still be
necessary for both the primary and secondary endpoint families.
IV. STATISTICAL METHODS
A variety of situations in which multiplicity arises have been discussed in sections II and III.
Statistical methods provide acceptable ways to correct for multiplicity and control the Type I
error rate for many of them. Standard statistical methods are available, for example:
• to examine treatment effects for multiple endpoints where success on any one endpoint
would be acceptable, and
• to allow sequential testing where success on one endpoint permits analysis of additional
endpoints.
1
This section describes methods that are commonly used for handling multiplicity problems in
controlled clinical trials that examine treatment effects on multiple endpoints.
A. Type I Error Rate for a Family of Endpoints and Conclusions on Individual
Endpoints
When there is a family of endpoints (discussed in sections II.A and III.A), the Type I error rate
commonly used for the group of study endpoints is called the family-wise Type I error rate
(FWER) or the overall Type I error rate for the family. The FWER is the probability of
erroneously finding a statistically-significant treatment effect in at least one endpoint regardless
of the presence or absence of treatment effects in the other endpoints within the family. This
error rate is typically held to 0.05 (0.025 for one-sided tests). The statistical methods discussed
in section IV.C maintain control of the FWER for finding significant treatment effects for study
endpoints individually, thereby permitting an individual effectiveness conclusion on each
endpoint.
There are also other statistical analysis methods, often called global procedures, that control the

899 FWER with regard to erroneously concluding that there is a treatment effect on some endpoint

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900 (one or more) when there is no such effect on any endpoint. These methods allow a conclusion 901 of treatment effectiveness in the global sense, but do not support reaching conclusions on the individual endpoints within the family. These methods are generally not encouraged when study 902 903 designs and methods that test the endpoints individually are feasible; therefore, these global 904 procedures are not described in this guidance. 905 906 Because composite and other multi-component endpoints (see sections III.C.3 and III.C.4) are 907 constructed as a single endpoint, when they are part of an endpoint family, the methods 908 described in section IV.C can be applied to them. 909 910 **B**. When the Type I Error Rate Is Not Inflated or When the Multiplicity 911 Problem Is Addressed Without Statistical Adjustment or by Other Methods 912 913 This section identifies two situations involving multiple endpoints where inflation of the Type I 914 error rate is avoided so that adjustments for multiplicity are not needed. These situations assume 915 that the trial has no interim analysis or mid-course design modifications. 916 917 1. *Clinically Relevant Benefits Required for All Specified Primary Endpoints — the* 918 Case of "Co-Primary" Endpoints¹⁴ 919 920 As discussed in detail in section III.C, when multiple primary endpoints are tested and success in 921 the study depends on success on all endpoints (i.e., they are co-primary endpoints), no 922 multiplicity adjustment is necessary because there is no opportunity to select the most favorable 923 result from among several endpoints. The impact of multiplicity in these situations is to increase 924 the Type II error rate (section III.B). 925 926 2. Use of Multiple Analyses Methods for a Single Endpoint after Success on the 927 Prespecified Primary Analysis Method 928 929 For many trials there are a range of plausible, closely related analyses of an individual endpoint. 930 For example, the primary analysis of an outcome trial could adjust for certain covariates, make a 931 different choice of covariates, make no covariate adjustment, be conducted on the intent-to-treat 932 (ITT) population or various modified populations, or use various hypothesis testing methods. 933 Accepting any one of these multiple analyses, when successful, as a basis for a conclusion that 934 there is a treatment effect would increase the study Type I error rate, but it is difficult to estimate 935 the increase in error rate because the results of these different analyses are likely to be similar 936 and it is unclear how many choices could have been made. As with other multiplicity problems, 937 prospective specification of the analysis method will generally eliminate the concern about a 938 biased (result-driven) choice. 939 940 Once the effect has been clearly demonstrated based on the prespecified primary analysis, 941 alternative analyses of the primary endpoint may be needed to correctly interpret the study's

⁹⁴² results. Additional analyses of the primary endpoint may be needed to gain a better

¹⁴ Section 505(d) of the FD&C Act.

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943 understanding of the observed treatment effect (e.g., to use a less conservative analysis to better 944 estimate the effect size). In other cases, multiple related analyses are used to assess the 945 sensitivity of the results to the important underlying assumptions of the prespecified analysis 946 method. For example, sensitivity analyses may be needed to determine the impact of missing 947 data on the primary analysis results, when the primary analysis method relies on unverifiable 948 assumptions about those missing data. Note that these additional analyses do not demonstrate 949 any new effects of the drug; rather, they clarify the effect already demonstrated by the primary 950 analysis of a successful study.

- 951
- 952 953

C. Common Statistical Methods for Addressing Multiple Endpoint-Related Multiplicity Problems

954 955 This section presents some common statistical methods and approaches for addressing 956 multiplicity problems in controlled clinical trials that evaluate treatment effects on multiple 957 endpoints. The choice of the method to use for a specific clinical trial will depend on the objectives and the design of the trial, as well as the knowledge of the drug being developed and 958 959 the clinical disorder. The method, however, should be decided upon prospectively. Because the 960 considerations that go into the choice of multiplicity adjustment method can be complex and 961 specific to individual product development programs, this guidance does not attempt to 962 recommend any one method over another in most cases. Sponsors should consider the variety of 963 methods available and in the prospective analysis plan select the most powerful method that is 964 suitable for the design and objective of the study and maintains Type I error rate control. There 965 are, for example, a small number of situations in which one method is unambiguously more 966 powerful than another without inflating the Type I error rate beyond the nominal level (e.g., the 967 Holm method is more powerful than the Bonferroni method for primary endpoints). These 968 situations are noted below.

969

970 The methods presented here are general, and the discussions and hypothetical examples have 971 been generally limited to two-arm trials that examine treatment versus control differences on 972 multiple endpoints. Similar considerations may apply to other kinds of multiplicity, such as in 973 assessing treatment effects at different time points, or at different doses. Although the following 974 discussions are oriented to the general reader, application of many of these methods can be 975 technically complex and should be used relying on statistical expertise. Consequently, when a 976 multiple endpoints problem arises in designing a clinical trial and one or more of these methods 977 are to be considered, consultation with knowledgeable experts is important.

978

979 Statistical methods for addressing multiplicity issues are broadly classified into two types: 980 single-step and multistep procedures. Single-step procedures provide for parallel (simultaneous) 981 testing and simultaneous (adjusted) confidence intervals for assessing the magnitude of the 982 treatment effects. Single-step procedures tend to cause loss of study power, so that sample sizes 983 need to be increased in comparison to sample sizes needed for a single-endpoint study. 984 Multistep procedures are generally more efficient in that they better preserve the power of the 985 tests, but do not readily provide adjusted confidence intervals. There are several kinds of 986 multistep procedures, for example step-down, step-up, and sequential procedures. 987

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988 In a step-down procedure, one calculates the p-values from all tests to be considered at one time 989 and starts hypothesis testing with the smallest p-value (i.e., statistically the most robust endpoint 990 test) and then steps down to the next smallest p-value (i.e., the next most robust endpoint test), 991 and so on. In a step-up procedure, one proceeds in the reverse direction. That is, one starts with 992 the largest p-value (i.e., the least robust test) and steps up to the second-largest p-value, finally 993 reaching the smallest p-value (i.e., the most robust test). These approaches are covered in the 994 following sections; e.g., the Holm procedure is a step-down procedure and the Hochberg 995 procedure is a step-up procedure.

996 997

1. The Bonferroni Method

998 999 The Bonferroni method is a single-step procedure that is commonly used, perhaps because of its 1000 simplicity and broad applicability. It is a conservative test and a finding that survives a 1001 Bonferroni adjustment is a credible trial outcome. The drug is considered to have shown effects 1002 for each endpoint that succeeds on this test. The Holm (section IV.C.2) and Hochberg (section 1003 IV.C.3) methods are more powerful than the Bonferroni method for primary endpoints and are 1004 therefore preferable in many cases. However, for reasons detailed in sections IV.C.2-3, sponsors 1005 may still wish to use the Bonferroni method for primary endpoints in order to maximize power 1006 for secondary endpoints or because the assumptions of the Hochberg method are not justified.

1007

1008 The most common form of the Bonferroni method divides the available total alpha (typically 1009 0.05) equally among the chosen endpoints. The method then concludes that a treatment effect is 1010 significant at the alpha level for each one of the *m* endpoints for which the endpoint's p-value is 1011 less than α/m . Thus, with two endpoints, the critical alpha for each endpoint is 0.025, with four 1012 endpoints it is 0.0125, and so on. Therefore, if a trial with four endpoints produces two-sided p-

values of 0.012, 0.026, 0.016, and 0.055 for its four primary endpoints, the Bonferroni method
would compare each of these p-values to the divided alpha of 0.0125. The method would

1015 conclude that there was a significant treatment effect at level 0.05 for only the first endpoint,

1016 because only the first endpoint has a p-value of less than 0.0125 (0.012). If two of the p-values

1017 were below 0.0125, then the drug would be considered to have demonstrated effectiveness on

1018 both of the specific health effects evaluated by the two endpoints.

1019

1020The Bonferroni method tends to be conservative for the study overall Type I error rate if the1021endpoints are positively correlated, especially when there are a large number of positively-

1022 correlated endpoints. Consider a case in which all of three endpoints give nominal p-values 1023 between 0.025 and 0.05, i.e., all 'significant' at the 0.05 level but none significant under the

Bonferroni method. Such an outcome seems intuitively to show effectiveness on all three

1025 endpoints, but each would fail the Bonferroni test. When there are more than two endpoints

1026 with, for example, correlation of 0.6 to 0.8 between them, the true family-wise Type I error rate 1027 may decrease from 0.05 to approximately 0.04 to 0.03, respectively, with negative impact on the

1028 Type II error rate. Because it is difficult to know the true correlation structure among different

1029 endpoints (not simply the observed correlations within the dataset of the particular study), it is

1030 generally not possible to statistically adjust (relax) the Type I error rate for such correlations.

1031 When a multiple-arm study design is used (e.g., with several dose-level groups), there are

1032 methods that take into account the correlation arising from comparing each treatment group to a

1033 common control group.

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1034	
1035	The Bonferroni test can also be performed with different weights assigned to endpoints, with the
1036	sum of the relative weights equal to 1.0 (e.g., 0.4, 0.1, 0.3, and 0.2, for four endpoints). These
1037	weights are prespecified in the design of the trial, taking into consideration the clinical
1038	importance of the endpoints, the likelihood of success, or other factors. There are two ways to
1039	perform the weighted Bonferroni test:
1040	
1041	• The unequally weighted Bonferroni method is often applied by dividing the overall alpha
1042	(e.g., 0.05) into unequal portions, prospectively assigning a specific amount of alpha to
1043	each endpoint by multiplying the overall alpha by the assigned weight factor. The sum of
1044	the endpoint-specific alphas will always be the overall alpha, and each endpoint's
1045	calculated p-value is compared to the assigned endpoint-specific alpha.
1046	
1047	• An alternative approach is to adjust the raw calculated p-value for each endpoint by the
1048	fractional weight assigned to it (i.e., divide each raw p-value by the endpoint's weight
1049	factor), and then compare the adjusted p-values to the overall alpha of 0.05.
1050	
1051	These two approaches are equivalent.
1052	
1053	2. The Holm Procedure
1054	
1055	The Holm procedure is a multi-step step-down procedure; it is useful for endpoints with any
1056	degree of correlation. It is less conservative than the Bonferroni method because a success with
1057	the smallest p-value (at the same endpoint-specific alpha as the Bonferroni method) allows other
1058	endpoints to be tested at larger endpoint-specific alpha levels than does the Bonferroni method.
1059	The algorithm for performing this test is as follows:
1060	
1061	The endpoint p-values resulting from the completed study are first ordered from the smallest to
1062	the largest. Suppose that there are m endpoints to be tested and $p_{(1)}$ represents the smallest p-
1063	value, $p_{(2)}$ the next-smallest p-value, $p_{(3)}$ the third-smallest p-value, and so on.
1064	
1065	i. The test begins by comparing the smallest p-value, $p_{(1)}$, to α/m , the same threshold used
1066	in the equally-weighted Bonferroni correction. If this $p_{(1)}$ is less than α/m , the treatment
1067	effect for the endpoint associated with this p-value is considered significant.
1068	
1069	ii. The test then compares the next-smallest p-value, $p_{(2)}$, to an endpoint-specific alpha of
1070	the total alpha divided by the number of yet-untested endpoints (e.g., $\alpha/[m-1]$ for the
1071	second smallest p-value, a somewhat less conservative significance level). If $p_{(2)} <$
1072	$\alpha/(m-1)$, then the treatment effect for the endpoint associated with this $p_{(2)}$ is also
1073	considered significant.
1074	-
1075	iii. The test then compares the next ordered p-value, $p_{(3)}$, to $\alpha/(m-2)$, and so on until the last
1076	p-value (the largest p-value) is compared to α .
1077	

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1078 iv. The procedure stops, however, whenever a step yields a non-significant result. Once an 1079 ordered p-value is not significant, the remaining larger p-values are not evaluated and it 1080 cannot be concluded that a treatment effect is shown for those remaining endpoints. 1081 1082 For example, when $\alpha = 0.05$, and there are four endpoints (m = 4), the significance level for the 1083 smallest p-value is $\alpha/m = 0.05/4 = 0.0125$, and significance levels for the subsequent ordered p-1084 values are $\alpha/(m-1) = 0.05/3 = 0.0167$, $\alpha/(m-2) = 0.05/2 = 0.025$, and $\alpha/(m-3) = 0.05/1 = 0.05$, 1085 respectively. 1086 1087 To illustrate, we apply the Holm procedure to the two-sided study result p-values used to explain 1088 the Bonferroni method: 0.012, 0.026, 0.016, and 0.055 associated with endpoints one to four, 1089 respectively (p_1, p_2, p_3, p_4) . With four endpoints, the successive endpoint-specific alphas are 1090 0.0125, 0.0167, 0.025, and 0.05. The smallest p-value in this group is $p_1 = 0.012$, which is less 1091 than 0.0125. The treatment effect for endpoint one is thus successfully demonstrated and the test 1092 continues to the second step. In the second step, the second smallest p-value is $p_3 = 0.016$, which 1093 is compared to 0.0167. Endpoint three has therefore also successfully demonstrated a treatment 1094 effect, as 0.016 is less than 0.0167. Testing is now able to proceed to the third step, in which the 1095 next ordered p-value of $p_2 = 0.026$ is compared to 0.025. In this comparison, as 0.026 is greater 1096 than 0.025, the test is not statistically significant. This non-significant result stops further tests. 1097 Therefore, in this example, this procedure concludes that treatment effects have been shown for 1098 endpoints one and three.

1099

1100 As noted, the Holm procedure is less conservative (and thereby more powerful) than the 1101 Bonferroni test. It tests the smallest p-value at the same alpha as the Bonferroni test, but, given a 1102 statistically-significant result on that endpoint, it tests subsequent p-values at higher significance 1103 levels. In the above example, the Bonferroni test was able to conclude that there is a significant 1104 treatment effect at the overall level 0.05 for endpoint one only; the Holm test was able to do so 1105 for endpoints one and three. Both, however, require at least one endpoint with a p-value < 1106 0.05/m. The Holm procedure is also more flexible than simple prospective ordering of endpoints 1107 for testing (section IV.C.5). It allows testing of the endpoint with the smallest p-value first, 1108 without knowing in advance which endpoint that will be. A disadvantage of the Holm procedure 1109 is the potential inability to pass along unused alpha (see section IV.C.6) to a secondary endpoint 1110 family because testing of any additional endpoints is not permitted when one of the sequentially-1111 tested endpoints in the family fails to reject the null hypothesis.

1112 1113

3. The Hochberg Procedure

1114

1115 The Hochberg procedure is a multi-step, step-up testing procedure. It compares the p-values to 1116 the same alpha critical values of α/m , $\alpha/(m-1)$, ..., α , as the Holm procedure, but, in contrast to 1117 the Holm procedure, the Hochberg procedure is a step-up procedure. Instead of starting with the 1118 smallest p-value, the procedure starts with the largest p-value, which is compared to the largest 1119 endpoint-specific critical value (α). Also, essentially in the reverse of the Holm procedure, if the 1120 first test of hypothesis does not show statistical significance, testing proceeds to compare the 1121 second-largest p-value to the second-largest adjusted alpha value, $\alpha/2$. Sequential testing 1122 continues in this manner until a p-value for an endpoint is statistically significant, whereupon the 1123 Hochberg procedure provides a conclusion of statistically-significant treatment effects for that

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1124 1125 1126 1127 1128 1129	endpoint and all endpoints with smaller p-values. For example, when the largest p-value is less than α , then the method concludes that there are significant treatment effects for all endpoints. In another situation, when the largest p-value is not less than α , but the second-largest p-value is less than $\alpha/2$, then the method concludes that treatment effects have been demonstrated for all endpoints except for the one associated with the largest p-value.
1129 1130 1131 1132	To illustrate, consider the same two-sided p-values used in the previous examples: 0.012, 0.026, 0.016, and 0.055 associated with endpoints one to four, respectively (p_1, p_2, p_3, p_4) .
1132 1133 1134 1135 1136	i. The largest p-value of $p_4 = 0.055$ is compared to its alpha critical value of $\alpha = 0.05$. Because this p-value of 0.055 is greater than 0.05, the treatment effect for the endpoint four associated with this p-value is considered not significant. The procedure, however, continues to the second step.
1137 1138 1139	ii. In the second step, the second largest p-value, $p_2 = 0.026$, is compared to $\alpha/2 = 0.025$; p_2 is also greater than the allocated alpha, and endpoint two associated with this p-value is also not statistically significant.
1140 1141	iii. In the third step, the next largest p-value, $p_3 = 0.016$, is compared to its alpha critical value of $\alpha/3 = 0.0167$, and this endpoint does show a significant treatment effect.
1142 1143 1144 1145	iv. The significant result on endpoint three automatically causes the treatment effect for all untested endpoints (which will have smaller p-values) to be significant as well (i.e., endpoint one in this case).
1143 1146 1147 1148 1149 1150 1151 1152 1153 1154 1155 1156 1157	Although for this specific example, the endpoints that are statistically significant are the same as for the Holm procedure, the Hochberg procedure is potentially more powerful. The Hochberg procedure may conclude that there are significant treatment effects for more endpoints than would the Holm procedure, depending on the specific p-values obtained in the study. This is because the Hochberg procedure allows testing of endpoints from the largest p-value to the smallest and concludes that all remaining endpoints are successful as soon as one test is successful, even if the remaining p-values would not have succeeded on testing with their appropriate sequential alpha level. In contrast, the Holm procedure tests from smallest p-value to largest and determines that all untested endpoints are unsuccessful as soon as one test is unsuccessful, even if those remaining endpoints would have been successful if tested with their appropriate sequential alpha level.
1158 1159 1160 1161 1162 1163 1164	Thus, for the case of two endpoints, if the two-sided p-values were 0.026 and 0.045, the Hochberg procedure will conclude that there are significant treatment effects on both endpoints, but the Holm procedure will fail on both. In the Hochberg procedure, the larger of the two p-values, $p = 0.045$ (< $\alpha = 0.05$), is a significant result, and the second endpoint is automatically considered significant. In the Holm procedure, the smaller of the two p-values, 0.026 (> $\alpha/m = 0.05/2$), is a non-significant result; therefore, the larger p-value is not evaluated.
1165 1166 1167	The Bonferroni and the Holm procedures are well known for being assumption-free. The methods can be applied without concern for the endpoint types, their statistical distributions, and the type of correlation structure. The Hochberg procedure, on the other hand, is not assumption-

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1168 free in this way. The Hochberg procedure is known to provide adequate overall alpha-control for 1169 independent endpoint tests and also for two positively-correlated dependent tests with standard 1170 test statistics, such as the normal Z, student's t, and 1 degree of freedom chi-square. It is also a 1171 valid test procedure when certain conditions are met. Various simulation experiments for the 1172 general case (e.g., for more than two endpoints with unequal correlation structures) indicate that 1173 the Hochberg procedure usually will, but is not guaranteed to, control the overall Type I error 1174 rate for positively-correlated endpoints, but fails to do so for some negatively-correlated 1175 endpoints. Therefore, beyond the aforementioned cases where the Hochberg procedure is known 1176 to be valid, its use is generally not recommended for the primary comparisons of confirmatory 1177 clinical trials unless it can be shown that adequate control of Type I error rate is provided.

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1180

4.

Prospective Alpha Allocation Scheme

1181 The Prospective Alpha Allocation Scheme (PAAS) is a single-step method that has a slight advantage in power over the Bonferroni method. The method allows equal or unequal alpha allocations to all endpoints, but, as with the Bonferroni method, each specific endpoint must receive a prospective allocation of a specific amount of the overall alpha. The alpha allocations are required to satisfy the equation:

1186 1187 1188

$$(1 - \alpha_1)(1 - \alpha_2) \dots (1 - \alpha_k) \dots (1 - \alpha_m) = (1 - \alpha).$$

1189 Each element in this equation, $(1 - \alpha_k)$, is the probability of correctly not rejecting the null hypothesis for the kth endpoint, when it is tested at the allocated alpha α_k . When the Type I error 1190 1191 rate for the study is set at 0.05 overall, the probability of correctly not rejecting any of the 1192 individual null hypotheses (i.e., when all null hypotheses are true) must be 1-0.05 = 0.95 = (1-1193 alpha). This equation states the requirement that probability of correctly not rejecting all of the 1194 individual null hypotheses, calculated by multiplying each of the m probabilities together, must 1195 equal the selected goal (e.g., 0.95). The alpha allocation for any of the individual endpoint tests 1196 can be arbitrarily assigned, if desired, but the total group of allocations must always satisfy the 1197 above equation. In general, when arbitrary alpha allocations are made for some endpoints, at 1198 least the last endpoint's alpha must be calculated in order to satisfy the overall equation. As 1199 stated earlier, the Bonferroni method relies upon a similar constraint-defining equation, except 1200 that for the Bonferroni method the sum of all the individual alphas must equal the overall study-1201 wise alpha.

1202

1203 Consider the case of three endpoints with two arbitrary alpha allocations in which $\alpha_1 = 0.02$ and 1204 $\alpha_2 = 0.025$ are assigned to the first two endpoints. If the total $\alpha = 0.05$, then the third endpoint would have an alpha of 0.0057, because the above equation becomes $(0.98)(0.975)(1 - \alpha_3) =$ 1205 0.95, so that $\alpha_3 = 0.0057$ for the third endpoint, instead of 0.005, as would have been assigned by 1206 1207 the Bonferroni method (0.02 + 0.025 + 0.005 = 0.05). When all alpha allocations are equal, then the individual comparison alpha is given by 1 - $(1 - \alpha)^{1/m}$. This adjustment formula is also known 1208 1209 as the Šidák adjustment formula. For the case of three endpoints, this adjusted alpha is 0.01695, 1210 which is only slightly greater than the 0.0167 assigned by the Bonferroni method. The slight 1211 savings in alpha provides a slight gain in the power of the tests. The PAAS ensures FWER 1212 control for all comparisons that are independent or positively correlated. If the endpoints are

1213 negatively correlated, FWER control may not be assured.

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5. The Fixed-Sequence Method

1217 The multiplicity problem arises from conducting tests for each of the multiple endpoints where 1218 each test provides an opportunity to decide that the study was successful. Any method that 1219 adequately adjusts for the multiplicity of opportunities will address the problem. In many 1220 studies, testing of the endpoints can be ordered in a specified sequence, often ranking them by 1221 clinical relevance or likelihood of success. A fixed-sequence statistical strategy tests endpoints 1222 in a predefined order, all at the same significance level alpha (e.g., $\alpha = 0.05$), moving to a second 1223 endpoint only after a success on the previous endpoint. Such a test procedure does not inflate the 1224 Type I error rate as long as there is (1) prospective specification of the testing sequence and (2) 1225 no further testing once the sequence breaks, that is, further testing stops as soon as there is a 1226 failure of an endpoint in the sequence to show significance at level alpha (e.g., $\alpha = 0.05$). 1227

1228 The idea behind this sequential testing method is that when there is a significant treatment effect 1229 for an endpoint, then the alpha level for this test remains available to be carried forward (passed

1230 along) to the next endpoint test in the sequence. However, the method uses all of the available

1231 alpha as soon as a non-significant result occurs. The order of testing is therefore critical.

1232

1233 The statistical conclusions provided by this method may differ from those provided by other 1234 methods, and they depend on the ordering of the tests. Consider, for example, a trial with three 1235 primary endpoints, A, B, and C, whose two-sided *p*-values for treatment effects are: $p_A = 0.045$, $p_B = 0.016$ and $p_C = 0.065$. This trial would conclude that there was a significant treatment effect 1236 for only the endpoint B by the Bonferroni test, because $p_B = 0.016 < 0.0167$ (i.e., 0.05/3), but 1237 1238 would not conclude that there was a significant effect on endpoints A or C. The Holm test would 1239 not find significant effects for additional endpoints either, unless the p-value for endpoint A was 1240 p < 0.025. If the study had planned sequential testing in the order of (C, B, A), it would be an 1241 entirely failed study, because $p_C = 0.065 > 0.05$, and no further testing would be performed after 1242 the first failed test for endpoint C. On the other hand, this trial would show significant treatment 1243 effects for endpoints B and A if it had planned sequential testing in the order of (B, A, C), because $p_B = 0.016 < 0.05$, and following it, $p_A = 0.045 < 0.05$; the same effects would be shown 1244 1245 if the order was (A, B, C). Thus, the fixed-order sequential testing method has the potential to 1246 find more endpoints successful than the single-step methods, but it also has the potential to find 1247 fewer endpoints successful, depending on the order chosen.

1248

1249 The appeal of the fixed-sequence testing method is that it does not require any alpha adjustment 1250 of the individual tests. Its main drawback is that if a hypothesis in the sequence is not rejected, a 1251 statistical conclusion cannot be made about the endpoints planned for the subsequent hypotheses, 1252 even if they have extremely small p-values. Suppose, for example, that in a study, the p-value 1253 for the first endpoint test in the sequence is p = 0.250, and the p-value for the second endpoint is 1254 p = 0.0001; despite the apparent "strong" finding for the second endpoint, no formal favorable 1255 statistical conclusion can be reached for this endpoint. Although it may seem counterintuitive to 1256 ignore such an apparently strong result, to allow a conclusion of drug effectiveness based on the 1257 second endpoint would in fact be ignoring the first endpoint's result and returning to the situation 1258 of having multiple separate opportunities to declare the study a success. Such a post hoc rescue

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recreates the multiplicity problem, and causes inflation of the study-wise Type I error rate. Theexample discussed here would, of course, have shown an effect using a Bonferroni test.

Thus, carefully selecting the ordering of the tests of hypotheses is essential. A test early in the
sequence that fails to show statistical significance will render the remainder of the endpoints not
statistically significant. It is often not possible to determine a priori the best order for testing,
and there are other methods for addressing the multiplicity problem, which are described in the
following subsections.

1267 1268

6. The Fallback Method

The fallback method is a modification of the fixed-sequence method that provides some
opportunity to test an endpoint later in the sequence even if an endpoint tested early in the
sequence has failed to show statistical significance. The order of the endpoints remains
important. The appeal of the fallback method is that if an endpoint later in the sequence has a
robust treatment effect while the preceding endpoint is unsuccessful, there is a modest amount of
alpha retained as a fallback to allow interpretation of that endpoint without inflating the Type I
error rate.

1277

1278 Applying the fallback method begins by dividing the total alpha (not necessarily equally) among 1279 the endpoints, and maintains a fixed sequence for the testing. As the testing sequence 1280 progresses, a successful test preserves its assigned alpha as "saved" (unused) alpha that is passed 1281 along to the next test in the sequence, as is the case for the sequential method. This passed-along 1282 alpha is added to the prospectively assigned alpha (if any) of that next endpoint and the summed 1283 alpha is used for testing that endpoint. Thus, as sequential tests are successful, the alpha 1284 accumulates for the endpoints later in the sequence; these endpoints are then tested with 1285 progressively larger alphas.

1286

To illustrate, consider a cardiovascular trial in which the first primary endpoint is exercise
capacity, for which the trial is adequately powered. The second primary endpoint is mortality,
for which the trial is underpowered.

- 1291i. Under the fallback method, we may assign $\alpha_1 = 0.04$ for the first endpoint test and save1292alpha of 0.01 for the second endpoint test. Any other desired division of the available1293overall alpha would also be permitted.
- 1294ii. If the first endpoint test is significant at level $\alpha_1 = 0.04$, this alpha is unused and is1295passed to the second endpoint test as an additional alpha of 0.04, giving a total alpha for1296the second endpoint test of 0.05 (0.01 + 0.04). The second endpoint test is then1297performed at the significance level of 0.05.
- iii. If the first endpoint is not significant at level 0.04, then this alpha of 0.04 is not
 available to be passed on for the second endpoint test. The test for the second endpoint
 is at the originally reserved alpha of 0.01.
- 1301

1302 In practice, users of this method usually assign most of the alpha to the first primary endpoint1303 and the remainder to the second endpoint, although other distributions are also valid. The

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1304 fallback method is often used when there is an endpoint thought less likely than another to be 1305 statistically significant, so that it is not designated the first endpoint, but is nevertheless of 1306 substantial clinical importance. The fallback method could conclude that an unexpectedly robust 1307 finding is statistically interpretable as a positive result even if the first primary endpoint failed, 1308 without inflation of the Type I error rate.

1309

1310 The statistical power of the fallback method depends primarily on the magnitude of the effect on, 1311 and alpha assigned to, each of the ordered endpoints. As with the simple fixed-sequence method, 1312 the overall power of the fallback method exceeds that of the Bonferroni test, because when the 1313 earlier endpoints show significant results, the method uses larger alpha levels for later endpoints than is possible under the Bonferroni method.

- 1314
- 1315 1316

7. Gatekeeping Testing Strategies

1317 1318 Clinical trials commonly assess efficacy of a treatment on multiple endpoints, usually grouped 1319 into a primary endpoint or endpoint family, and a secondary endpoint or endpoint family (see 1320 sections II.A and III.A). The usual strategy is to test all endpoints in the primary family 1321 according to one of the previously discussed methods (e.g., Bonferroni, fallback) and proceed to 1322 the secondary family of endpoints only if there has been statistical success in the primary family. 1323 This allows all of the available alpha level to be distributed within the primary family 1324 (containing the most important study endpoints) and thus maximizes the study power for those 1325 endpoints. In contrast, if the available alpha were distributed among all of the endpoints in the 1326 primary and secondary families, power would be reduced for the primary endpoints. Although it 1327 is not generally recommended, if there were an additional family of endpoints for which it was 1328 also important to control the Type I error rate, that family could be designated as third in the 1329 sequence.

1330

1331 This approach of testing the primary family first, and then the secondary family contingent upon 1332 the results within the primary family is called the gatekeeping testing strategy to highlight the 1333 fact that the endpoint families are analyzed in a sequence, with each family serving as a 1334 gatekeeper for the next one. The tests for the secondary family (and subsequent families if any) 1335 are carried out with appropriate multiplicity adjustments within that family, but only if the tests 1336 in the primary family have been successful.

1337

1338 Two types of gatekeeping testing strategies are common in clinical trials, serial and parallel, 1339 determined by how the endpoints are tested within the primary family. The term serial strategy 1340 is applied when the endpoints of the primary family are tested as co-primary endpoints (section 1341 III.C). If all endpoints in the primary family are statistically significant at the same alpha level 1342 (e.g., $\alpha = 0.05$), the endpoints in the second family are examined. The endpoints in the second 1343 family are tested by any one of several possible methods (e.g., Holm procedure, the fixed-1344 sequence method, or others described in section IV.C). If, however, at least one of the null 1345 hypotheses of the primary family fails to be rejected, the primary family criterion has not been 1346 met and the secondary endpoint family is not tested.

1347

1348 The term parallel gatekeeping strategy is applied when the endpoints in the primary family are 1349 not all co-primary endpoints, and a testing method that allows the passing along of alpha from an

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- 1350 individual test to a subsequent test (e.g., Bonferroni method or Truncated Holm method 1351 described next) is specified. In this strategy, the second endpoint family is examined when at 1352 least one of the endpoints in the first family has shown statistical significance. 1353 1354 The Bonferroni method is sometimes used for the parallel gatekeeping strategy, as it is the 1355 simplest approach. The secondary endpoint family may use a different method (e.g., the fixed-1356 sequence method or Holm method). In this approach, if an endpoint comparison within the 1357 primary family is statistically significant at its allocated (or accumulated) endpoint-specific alpha 1358 level, then this alpha level can be validly passed on to the next family. On the other hand, if an 1359 endpoint comparison in a family is not significant at its endpoint-specific alpha level, that alpha 1360 is not passed on to the next family. The overall alpha available for testing the secondary family 1361 is the accumulated (unused) endpoint-specific alpha levels of those comparisons in the primary 1362 family that were found significant. 1363 1364 To illustrate, consider a trial whose primary objective is to test for superiority of a treatment to 1365 placebo for five endpoints: A, B, C, D and E. For this objective, the trial organizes the endpoints 1366 hierarchically into a primary family $F1 = \{A, B\}$ and a secondary family $F2 = \{C, D, and E\}$. 1367 The statistical plan is to assign the total available alpha (0.05) to F1 and test the endpoints A and 1368 B in F1 by the Bonferroni method at endpoint-specific alpha levels of 0.04 and 0.01, 1369 respectively. No alpha is reserved for the second family, and the second family is tested with the 1370 Holm procedure with whatever amount of alpha is passed along to it. If, at the completion of the 1371 tests for F1, the p-values for the endpoints A and B are 0.035 and 0.055, respectively, and the p-1372 values for endpoints C, D and E are 0.011, 0.045, and 0.019, respectively, then: 1373 1374 i. The result for endpoint A is significant, but the result for endpoint B is not, leaving 1375 alpha of 0.04 as unused and alpha of 0.01 as used. 1376 ii. The total alpha available for testing the endpoints in F2 is 0.04 and not 0.05. 1377 iii. The endpoints C and E are significant at level 0.04 by the Holm test (C, E, and D are 1378 tested at levels of 0.0133, 0.02, 0.04, respectively). 1379 1380 The gatekeeping method described above controls the study-wise Type I error rate (e.g., at level 1381 0.05) associated with the trial's primary and secondary families. The study-wise Type I error 1382 rate takes into consideration the potential for an erroneous conclusion of efficacy for any 1383 endpoint in any family and the multiple possibilities of the drug being truly effective or 1384 ineffective on any of the endpoints. The gatekeeping strategy controls the study-wise Type I 1385 error rate when the principle of passing along only unused alpha from statistically-significant 1386 tests of hypotheses is applied. In contrast, however, independent error rate control of each 1387 family's FWER (i.e., testing each family at a separate 0.05) can lead to inflation of the study-1388 wise Type I error rate when some, but not all, of the null hypotheses for the primary endpoint 1389 family are in fact true. 1390 1391 8. The Truncated Holm and Hochberg Procedures for Parallel Gatekeeping 1392 1393 When used as a gatekeeping strategy to test the primary family of endpoints, the Bonferroni
- 1394 method and some other single-step methods (such as the Dunnett's test, which is not covered in

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1395 this document) have an important property of preserving some alpha for testing the secondary 1396 endpoint family when at least one of the endpoints in the primary family is statistically 1397 significant. In the Bonferroni method, the endpoint-specific alpha from each test that 1398 successfully rejected that null hypothesis is summed and becomes the alpha available to the 1399 secondary endpoint family. For example, in the equally weighted Bonferroni method, when 1400 there are two endpoints in the primary family, the unused alpha available for tests of hypotheses 1401 in the secondary family can be 0.05, 0.025, or 0, depending, respectively, on whether both, one, 1402 or none of the primary endpoint tests rejected their respective null hypotheses.

1403

The conventional Holm and Hochberg methods, however (see sections IV.C.2 and IV.C.3), do not have this property. These methods pass alpha from the primary family to the secondary family only when all of the null hypotheses in the primary family are rejected. These two methods give better power on recycling all alpha within the family and releasing it only when all hypotheses in that family are rejected. Inappropriately proceeding as if there is some preserved alpha when a study fails to reject one or more of the primary hypotheses will result in an inflated overall Type I error rate.

1411

1412 There are, however, procedures called the truncated Holm and the truncated Hochberg that can

1413 be used when there is a desire to have the power advantage of the conventional Holm or

1414 Hochberg procedures but also to have some alpha available for testing the secondary endpoint

1415 family if at least one of the primary endpoints is successful. In a truncated Holm or Hochberg 1416 procedure, some portion of the unused alpha from each step is reserved for passing to the

1416 procedure, some portion of the unused alpha from each step is reserved for passing to the 1417 secondary endpoint family. The truncated Holm procedure and the truncated Hochberg

1418 procedures are hybrids of their conventional forms and the Bonferroni method. As a

1419 consequence, the endpoint-specific alpha for each successive test of hypothesis of the primary

1420 endpoints after the first is not as large as in the conventional Holm or the conventional Hochberg

1421 procedure. In either of these approaches, of course, if all of the individual endpoint tests of

1422 hypotheses in the primary endpoint family successfully reject the null hypothesis, the full alpha

1423 of 0.05 is available for the secondary endpoint family. The amount of reserved alpha from the

successive tests should be chosen carefully, as the choice creates a balance between decreasing study power for the endpoints in the primary family and the guarantee (if at least the first test

- rejects the null hypothesis) of some power to test the secondary endpoint family. The following
- 1427 example illustrates these two procedures for a primary family with three endpoints.
- 1428

1429 Consider treatment versus control comparisons for three endpoints in the primary family with the 1430 control of alpha at the 0.05 level. The endpoint-specific alpha levels for the conventional Holm 1431 for this case are 0.05/3, 0.05/2, and 0.05 (see section IV.C.2), and those by the equally weighted 1432 Bonferroni method are 0.05/3, the same for each comparison (see section IV.C.1). The endpoint-1433 specific alpha levels for the truncated Holm are then constructed by combining the endpoint-1434 specific alpha levels of the two methods with a "truncation fraction" of f, whose value between 1435 zero and one is selected in advance. The following calculations illustrate this combination using 1436 f = 1/2; the multipliers with f are the endpoint-specific alpha levels for the conventional Holm and 1437 those with (1-f) are by the equally weighted Bonferroni method.

1438

$$\alpha_{1} = \frac{0.05}{3}f + \frac{0.05}{3}(1-f) = \frac{0.05}{3} \cdot \frac{1}{2} + \frac{0.05}{3}(1-\frac{1}{2}) = 0.0167$$

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1440

$$\alpha_{2} = \frac{0.05}{2}f + \frac{0.05}{3}(1-f) = \frac{0.05}{2} \cdot \frac{1}{2} + \frac{0.05}{3}(1-\frac{1}{2}) = 0.0208$$

$$\alpha_{3} = \frac{0.05}{1}f + \frac{0.05}{3}(1-f) = \frac{0.05}{1} \cdot \frac{1}{2} + \frac{0.05}{3}(1-\frac{1}{2}) = 0.0333$$

1441 1442

1443 Thus, for this particular case, when the value of f = 1/2, the first test for the truncated Holm test 1444 is performed at $\alpha_1 = 0.0167$, which is the same for the conventional Holm test. However, the 1445 second test, after the first test is successful, is performed at level $\alpha_2 = 0.0208$, and the third test, 1446 after the first two tests are successful, is at level $\alpha_3 = 0.0333$. The unused alpha levels for passing 1447 to the secondary family are calculated as:

- 1448
- 1449

i. Unused alpha = 0.05, if all three tests are successful;

- 1450ii. Unused alpha = $(0.05 \alpha_3) = 0.05 0.0333 = 0.0167$, if the first two tests are successful,1451but the last one is not;
- 1452 1453

iii. Unused alpha = $(0.05 - 2\alpha_2) = 0.05 - 2(0.0208) = 0.0084$, if the first test is successful, but the other two tests are not.

1454

1455 For the truncated Hochberg, alpha levels α_1 , α_2 , and α_3 are the same as those for the truncated 1456 Holm, except that for the truncated Hochberg, the first test starts with the largest p-value (i.e., 1457 largest of the three endpoint treatment-to-control comparison p-values) at level $\alpha_3 = 0.0333$. If 1458 this first test is successful, then the other two tests are also considered successful, and alpha of 1459 0.05 passes to the secondary family. However, if the first test is not successful, then the second 1460 test with second-largest p-value is at level $\alpha_2 = 0.0208$. If this second test is successful, then the 1461 remaining last test is also considered successful, and alpha of 0.0167 passes to the secondary 1462 family. However, if this second test is not successful, then the last test with the smallest p-value is at level $\alpha_1 = 0.0167$, and if that test is successful, then alpha of 0.0084 passes to the secondary 1463 1464 family. This illustration is with f = 1/2. Similar calculations would follow for different values of 1465 f.

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- 1467 1468

9. Multi-Branched Gatekeeping Procedures

Some multiplicity problems are multidimensional. One dimension may correspond to multiple endpoints, a second to multiple-dose groups (that have each of those endpoints tested), and yet another dimension to multiple hypotheses regarding an endpoint, such as non-inferiority and superiority tests (for each dose and each endpoint). Each individual hypothesis to test pertains to one particular endpoint, dose, and analysis objective. The total number of hypotheses is the product of the number of options within each dimension and can become large, even when there are only two or three options for each dimension.

1476

1477 The multiple sources of multiplicity create the potential for multiple pathways of testing the

1478 hypotheses. For example, if the goal of a study is to demonstrate non-inferiority as well as

1479 superiority, a single path of sequential tests is preferred. After demonstrating non-inferiority on

1480 the endpoint, it is possible to then test for superiority at an unadjusted alpha. In a fixed-sequence

1481 (unbranched) approach, it would also be appropriate to analyze a second endpoint for non-

1482 inferiority at the same alpha after the first endpoint is successfully shown to be non-inferior.

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1483 Suppose, however, that one wants to carry out both of these analyses after showing non-1484 inferiority for the first endpoint. The testing path now branches into two paths from this initial test, i.e., testing superiority for the first endpoint and non-inferiority for the second endpoint. 1485 1486 There is a choice of statistical adjustments to apply in this setting. 1487 1488 Treating the hypotheses as independent and applying a simple method such as Bonferroni leads 1489 to testing these hypotheses at small alpha levels, and consequently a very large study may be 1490 necessary to ensure good study power. Alternatively, applying a fixed-sequence method may 1491 lead to many endpoint tests being disallowed because the optimal sequence for testing is usually 1492 not prospectively determinable. The multi-branched gatekeeping procedure can address 1493 multiplicity problems of this multi-dimensional type. The multi-branched gatekeeping procedure 1494 allows for ordering the sequence of testing with the option of testing of more than one endpoint 1495 if a preceding test is successful. When there are multiple levels of this sequential hierarchy, and 1496 branching is applied at several of the steps, the possible paths of endpoint testing become a 1497 complex, multi-branched structure. 1498 1499 As a simple illustration (Figure 1), consider a clinical trial that compares a treatment to control 1500 on two primary endpoints (endpoint one and endpoint two) to determine first whether the 1501 treatment is non-inferior to the control for at least one endpoint. If, for either of the two

endpoints, the treatment is found non-inferior to the control, there is also a desire to test whether
it is superior to control for that endpoint. The analytic plan for the trial thus sets the following
logical restrictions:

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- i. Test endpoint two only after non-inferiority for endpoint one is first established.
- ii. Test for superiority on an endpoint only after non-inferiority for that endpoint is first concluded.
- 1510 The following diagram shows the decision structure of the test strategy. In this diagram, each 1511 block (or node) states the null hypothesis that it tests.
- 1512



- 1513 1514
- 1515 Figure 1: Example of a flow diagram for non-inferiority and superiority tests for endpoints one and two of a trial
- 1516 with logical restrictions: in order to test for superiority for endpoint one and/or two, one must first establish non-1517 inferiority for that endpoint.
- 1518

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Thus, the above test strategy has a two-dimensional hierarchical structure, one dimension for the two different endpoints and the other for the non-inferiority and superiority tests, with the logical restrictions as stated above. A different study might have three dimensions, two endpoints to be tested at two dose levels (along with a control group) with non-inferiority and superiority tests on each endpoint, having restrictions, e.g., that the lower dose can be tested after a success on the higher dose, and superiority on an endpoint can be tested after non-inferiority has been shown.

1525

1526 For the test strategy in Figure 1, one may, inappropriately, test each hypothesis at the same

- 1527 significance level (e.g., $\alpha = 0.05$), reasoning that the tests for non-inferiority for the two 1528 endpoints follow a sequential order, allowing passing along the full alpha; and that the test for
- 1529 superiority for each endpoint follows naturally after non-inferiority for it is first demonstrated.
- 1530 This approach, however, is likely to inflate the overall Type I error rate, because in Figure 1, the
- 1531 testing path (sequence) after the node at H_1 splits into two branches; one goes on to test for H_2
- and the other to test for H_3 . Consequently, once the trial concludes non-inferiority of the
- treatment to control for endpoint one, erroneous conclusions for tests of H_2 and H_3 can occur in
- multiple ways; that is, either H_2 is erroneously rejected, or H_3 is erroneously rejected, or both H_2
- 1535 and H_3 are erroneously rejected. If each of these separate hypotheses were to be tested at the
- 1536 0.05 level, this would obviously lead to Type I error rate inflation. As another illustration of 1537 Type I error rate inflation, suppose that in reality the treatment is non-inferior to control for both
- Type I error rate inflation, suppose that in reality the treatment is non-inferior to control for both endpoints but is not superior to control for either endpoint. In this scenario, the testing scheme
- 1539 (without alpha adjustments) can conclude superiority of the treatment to control in multiple
- 1540 ways, i.e., the treatment is superior to control for either endpoint one or endpoint two, or for both 1541 endpoints.
- 1542

1543 It is possible to deal with this problem using the Bonferroni-based gatekeeping method by1544 grouping the hypotheses as follows:

- 1545
- Group one includes only H_1 (the test of non-inferiority for endpoint one)
- Group two includes H_2 (the test of superiority for endpoint one) and H_3 (the test of noninferiority for endpoint two)
- Group three includes only H_4 (the test of superiority for endpoint two).
- 1550

1551 The procedure would begin with the test of the single hypothesis H_1 in group one at the level 1552 intended for the study-wise overall Type I error rate (e.g., $\alpha = 0.05$). Group one serves as a 1553 gatekeeper for group two. Therefore, once the result for H_1 is significant at level α (i.e., the

1554 treatment is non-inferior to control for endpoint one at level α), testing proceeds to the

- 1555 hypotheses H_2 and H_3 in group two with the alpha that was not used within family one, which in
- 1556 this case would be the overall study alpha.
- 1557
- 1558 The test of H_2 and H_3 in family two can use the Bonferroni method at the endpoint-specific alpha
- 1559 of 0.025 for each test according to the Bonferroni-based gatekeeping method. The standard
- 1560 Holm procedure is not considered here for the reason discussed in sections IV.C.2 and IV.C.8.
- 1561 Dividing the available alpha between the two endpoints will reduce study power for these
- 1562 endpoints (or necessitate an increased sample size to maintain study power), making it more
- 1563 difficult for the study to succeed on these endpoints; but it is necessary to maintain control of
- 1564 Type I error rate.

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1565 1566 Therefore, if both H₂ and H₃ are rejected, H₄ is tested at $\alpha = 0.05$. However, if only H₃ is rejected, then H₄ is tested at $\alpha = 0.025$. If H₃ is not rejected but H₂ is rejected, H₄ could be tested 1567 at $\alpha = 0.025$ in accord with the plan, but this would be illogical because if endpoint two failed to 1568 1569 show non-inferiority (H_3) , superiority could not have occurred. 1570

1571 When there are three or more dimensions and multiple branch points, planning the sequence of 1572 testing becomes complex and difficult to describe in the manner illustrated here. In these 1573 situations, the graphical approach to displaying and evaluating analysis paths (Appendix A) can 1574 be valuable.

1575 1576

10. Resampling-Based, Multiple-Testing Procedures

1577 1578 When there is correlation among multiple endpoints, resampling is one general statistical 1579 approach that can provide more power than the methods described above to detect a true 1580 treatment effect while maintaining control of the overall Type I error rate, and the power 1581 increases as the correlation increases. With these methods, a distribution of the possible test-1582 statistic values under the null hypothesis is generated based upon the observed data of the trial. 1583 This data-based distribution is then used to find the p-value of the observed study result instead 1584 of using a theoretical distribution of the test statistics (e.g., a normal distribution of Z-scores, or a 1585 t-distribution for t-scores) as with most other methods.

1586

1587 Resampling methods include the bootstrap and permutation approaches for multiple endpoints 1588 and require few, albeit important, assumptions about the true distribution of the endpoints. There 1589 are, however, some drawbacks to these methods. The important assumptions are generally 1590 difficult to verify, particularly for small study sample sizes. These methods, consequently, 1591 usually require large study sample sizes (particularly bootstrap methods) and often require 1592 simulations to ensure the data-based distribution of the test statistics from the limited trial data is 1593 applicable and to ensure adequate Type I error rate control. Inflation of the Type I error rate may 1594 occur, for example, if the shape of the data distribution is different between the treatment groups being compared. 1595 1596

1597 There is at present little experience with these methods in drug development clinical trials.

1598 Because of this, resampling methods are not recommended as primary analysis methods for

1599 adequate and well-controlled trials in drug development. It may, however, be useful and

1600 instructive to compare the results of resampling methods with those obtained using conventional

1601 methods in order to gain experience with and understanding of resampling methods' properties, advantages, and limitations.

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- 1603 1604

1605 V. **CONCLUSION**

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1607 The chance of making a false positive conclusion, concluding that a drug has a beneficial effect 1608 when it does not, is of primary concern to FDA. The widely accepted standard is to control the 1609 chance of coming to a false positive conclusion (Type I error probability) about a drug's effects

1610 to less than 2.5 percent (1 in 40 chance). As the number of endpoints or analyses increases, the

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probability of making a false positive conclusion can increase well beyond the 2.5 percent 1611 1612 standard. Multiplicity adjustments, as described in this guidance, provide a means for 1613 controlling Type I error when there are multiple analyses of the drug's effects. There are many 1614 strategies and/or choices of methods that may be used, as appropriate, as described in this 1615 guidance. Each of these methods has advantages and disadvantages and the selection of suitable 1616 strategies and methods is a challenge to be addressed at the study-planning stage. Statistical 1617 expertise should be enlisted to help choose the most appropriate approach. Failure to 1618 appropriately control the Type I error rate can lead to false positive conclusions; this guidance is 1619 intended to clarify when and how multiplicity due to multiple endpoints should be managed to 1620 avoid reaching such false conclusions.

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APPENDIX: THE GRAPHICAL APPROACH

1693 1694 A graphical approach is available for developing and evaluating hierarchal multiple analysis 1695 strategies. This approach provides a means for specifying, communicating, and assessing 1696 different hypothesis testing strategies, but is not by itself an additional method for addressing 1697 multiplicity (such as those described in section IV). Instead, the graphical approach is a means 1698 of depicting a strategy consisting of the previously described Bonferroni-based sequential 1699 methods, such as fixed-sequence, fallback type, and gatekeeping procedures. This approach 1700 illustrates differences in endpoint importance as well as the relationships among the endpoints by 1701 mapping onto a test strategy that ensures control of the Type I error rate and aids in creating and 1702 evaluating alternative test strategies. This technique will be most helpful when the analysis plan 1703 is complex due to splitting of the overall alpha among several endpoints (either initially or after a 1704 particular endpoint has been successful), particularly if there is a desire to have a second chance 1705 for an endpoint that was not statistically significant at the initially assigned endpoint-specific 1706 alpha, but can receive pass-along alpha from a different endpoint that was successful (the loop-1707 back feature described below). This situation may occur when complex testing strategies are

being considered because of intricate endpoint relationships and differing endpoint importance.

Graphical displays of complex analysis strategies can aid in clearly describing and assessing the proposed plan by displaying all the logical relationships among endpoint tests of hypotheses. In addition, simple modifications of the initial graph can easily create different variations of a test strategy, aiding comparison among the variations. The graphical approach can be useful in trial design to identify a test scheme that is suitably tailored to the objectives of the trial.

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1692

1716 Basics of the Graphical Approach: Use of vertex (node) and path (order or direction) 1717

1718 In the graphical approach, the testing strategy is defined by a figure that shows each of the 1719 hypotheses $(H_1, H_2, ..., H_m)$ located at a vertex (or node, a junction of testing order paths), and 1720 depicts the test order paths by lines (with the direction of the path indicated by an arrowhead) 1721 connecting the hypotheses. Each vertex (hypothesis) is allocated an initial amount of alpha, 1722 which we call here the "endpoint-specific alpha" (with the understanding that a test of an 1723 endpoint is associated with a test of a hypothesis, and vice versa). A key requirement is that the 1724 sum of all of the endpoint-specific alpha levels is equal to the total alpha level available for the study (the study-wise Type I error rate). An exception can occur if one designates two or more 1725 1726 hypotheses as a co-endpoint group, so that the same endpoint-specific alpha is applied to all tests 1727 in that group.

1728

Each test order path is also assigned a value between 0 and 1, called a weight for that path and
shown above the arrow, which indicates the fraction of the preserved alpha to be shifted along
that path to the receiving hypothesis, when the hypothesis at the tail end of the path is successful
(i.e., is rejected). The sum of the weights across all the paths leaving a vertex must be 1.0, so
that the entire preserved alpha is used in testing subsequent hypotheses.

- 1734
- 1735 All study hypotheses that are intended to potentially provide firm conclusions of efficacy are
- shown in the graph. With this technique there is no need to explicitly designate hypotheses as
- 1737 part of the primary or secondary endpoint families; more nuanced hierarchies are able to be

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achieved based on the initial allocation of the endpoint-specific alpha and the division of passed-

- 1739 forward alpha among the test paths leaving each vertex. Clearly, the hypotheses that receive an
- 1740 initial endpoint-specific alpha allocation of 0.0 will often be those regarded as of lesser
- importance, which is implicitly similar to designating the associated endpoint as a secondaryendpoint.
- 1743

1744 Adhering to the principles outlined in prior sections of this guidance, when an endpoint test is

- successful in rejecting the corresponding null hypothesis, that endpoint-specific alpha can be passed on to the next test indicated by the arrow, and will be divided among several subsequent
- 1747 hypotheses when there are several paths leaving that vertex. This shift of alpha occurs only
- when the test result for the hypothesis associated with a vertex at the arrow's tail is significant.
- 1749 Thus, as with the simple fallback method, the actual endpoint-specific alpha used in an endpoint 1750 test cannot be determined until the study results are complete and hypothesis testing begins; the
- 1750 test cannot be determined until the study results are complete and hypothesis testing begins; th 1751 sequential test determines which vertices are associated with alpha levels that can be passed
- 1752 along for accumulation in the subsequent test and which are not.
- 1753

1754 Several examples of the graphical method follow to help illustrate the concept, construction,

interpretation, and application of these diagrams. The first several of these examples are simple

1756 cases where the graphical approach is no more useful than a nondiagramatic (written text)

1757 description, but where the principles of the approach can be more clearly illustrated.

1758

1759 Fixed-Sequence Method

1760
1761 The fixed-sequence testing strategy (section IV.C.5), shown in Figure A1, illustrates a simple
1762 case of the graphical method with three hypotheses. In this scheme, the endpoints (hypotheses)
1763 are ordered. Testing begins with the first endpoint at the full alpha level, and continues through

the sequence only until an endpoint is not statistically significant. This diagram shows that the endpoint-specific alpha levels associated with hypotheses H₁, H₂, and H₃ are set in the beginning as α , 0, and 0. Arrows indicate the sequence of testing, and if the test is successful, the full alpha is shifted along to the next test. Consequently, if null hypothesis H₁ is successfully rejected, the endpoint-specific alpha level for H₂ becomes 0 + 1 x $\alpha = \alpha$, which allows testing of H₂ at level α . However, if the test of H₁ is unsuccessful, there is no pre-assigned non-zero alpha for H₂ to allow testing of H₂, so the testing stops.



1772 1773 1774 1775

Figure A1: Graphical illustration of the fixed-sequence testing with three hypotheses.

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1776 Loop-Back Feature to Indicate Two-Way Potential for Alpha Passing

1777 1778 Another valuable feature of the graphical method occurs when the available alpha level is split between two or more endpoints into endpoint-specific alphas levels; these diagrams can easily 1779 1780 illustrate the potential for loop-back passing of endpoint-specific alpha. If a hypothesis is not 1781 rejected at its endpoint-specific alpha level, but a different hypothesis is, then the unused 1782 endpoint-specific alpha from the rejected second hypothesis can be directed to loop back to the 1783 first hypothesis, which is then re-tested at the higher alpha level. Thus, in Figure A2, if assigned 1784 endpoint-specific alpha levels for testing H₁ and H₂ are $\alpha_1 = 0.04$ and $\alpha_2 = 0.01$, respectively, and 1785 if H_1 is not rejected but H_2 is rejected, then the unused alpha of 0.01 for H_2 loops back to H_1 for 1786 re-testing at the higher level of 0.04 + 0.01 = 0.05. Without the loop-back from H₂ to H₁ this

1787 would simply be the fallback method (described in section IV.C.6).

1788



1789 1790

1791Figure A2: Graphical illustration of the loop back passing of endpoint-specific alpha from H_2 to1792 H_1 .

1793

1794 The Holm procedure (section IV.C.2) is a specific case of tests for two hypotheses with a loop-1795 back feature where the graphical method enables a simple depiction of the procedure and its 1796 rationale. The Holm procedure directs that the first step is to test the smaller p-value at endpoint-1797 specific alpha = $\alpha/2$ and, only if successful, proceed to test the larger p-value at the level α (e.g., 1798 0.05). Because the Holm procedure splits alpha evenly in half, if the test of hypothesis with the 1799 smaller p-value was not significant, it is clear that the test with the larger p-value will also fail to 1800 be significant; performing that comparison is unnecessary. The diagram for the Holm procedure 1801 (Figure A3), shows two vertices and associated endpoint-specific alpha levels of $\alpha_1 = 0.025$ and 1802 $\alpha_2 = 0.025$, respectively, satisfying the requirement for total alpha = 0.05. The two arrows show 1803 that alpha might be passed along from H_1 to H_2 , or H_2 to H_1 . If the first test is successful, the 1804 endpoint-specific alpha of 0.025 is shifted entirely to the other hypothesis, and added to the 1805 endpoint-specific alpha already allocated for that hypothesis to provide a net alpha of 0.05. 1806 Because either hypothesis might be tested first, the diagram shows a loop-back configuration.

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1808

1809

1810 Figure A3: Graphical illustration of the Holm procedure with two hypotheses.

1811

1812 Because of the loop-back procedure and potential for retesting at a larger accumulated endpoint-

1813 specific alpha, the figure shows that there is no need for the Holm procedure's rule of starting 1814 with the smaller p-value. Testing can begin at either vertex because the other vertex can always

1815 be tested, and the first vertex can be retested if it did not succeed on first examination. Both will

1815 be tested, and the first vertex can be refested if it did not succeed on first examination. Both w

1816 have an endpoint-specific alpha of at least 0.025, and if one vertex's test is successful, the other

hypothesis will be tested (or retested) at the full alpha of 0.05. This is a general principle foranalysis strategies described with the graphical approach. Testing on the diagram with loop-back

1818 may start at any of the vertices that have non-zero alpha in the initial diagram, and all vertices

1820 with non-zero alpha can be tested until one is found for which the test is successful (i.e., the

1821 hypothesis is rejected). Testing then follows the arrows, passing the alpha along as directed in the diagram. The final conclusions of which hypotheses were statistically configurate and which

the diagram. The final conclusions of which hypotheses were statistically significant and which were not will be the same irrespective of which vertex was inspected first. The graphical method enables complex alpha-splitting and branching of testing path features to be clearly identified as part of the analysis plan and correctly implemented.

1826

1827 An Improved Fallback Method

1828

1829 Figure A4 (a) displays the conventional fallback test (section IV.C.6) with three hypotheses.

1830 Each of the hypotheses is assigned an endpoint-specific alpha so that their sum $\alpha_1 + \alpha_2 + \alpha_3 = \alpha_1$ If

1831 the test result for H_1 is significant, then its level α_1 is passed on to H_2 , as indicated by the arrow 1832 going from H_1 to H_2 . Furthermore, if the test result for H_2 is now significant at its endpoint-

specific alpha level (which will be either α_2 or $\alpha_1 + \alpha_2$), then this level is forwarded to H₃ as

indicated by the arrow going from H_2 to H_3 . Thus, if test results for both H_1 and H_2 are

1835 significant, then the total alpha level available for the test of H₃ is $\alpha_1 + \alpha_2 + \alpha_3 = \alpha$.

1836

1837 Examination of the conventional fallback method suggests an improvement, as shown in Figure 1838 A4 (b). In the conventional scheme, if the test result for H_3 is significant, then its endpoint-

1838 A4 (b). In the conventional scheme, if the test result for H_3 is significant, then its endpoint-1839 specific alpha level is not shifted to any other hypothesis. Hypothesis H_3 , however, is permitted

specific alpha level is not shifted to any other hypothesis. Hypothesis H_3 , however, is permitted to be tested even if the test of H_2 were not successful. In the case where the test result for H_3 is

significant, its endpoint-specific alpha level can be re-used either by H_1 or H_2 or both (if loop-

back of the endpoint-specific alpha level of H_3 was divided between H_1 and H_2). Thus, two

1843 loop-back arrows can be added to the conventional fallback figure to show the potential for

1844 passing back of some portion of H_3 's endpoint-specific alpha to H_1 , H_2 , or both. The actual

1845 fraction to be passed back to H_1 , and the fraction to H_2 , should be prospectively specified, and

1846 cannot be adjusted after the study results are examined (when it could be seen which of the two

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earlier endpoints might most benefit from this passing-back of alpha). Figure A4(b) shows this procedure with the fraction r of this un-used alpha shifted to H_2 and the remaining fraction 1- r of this alpha shifted to H_1 . The value of r should be prospectively specified in the study analysis plan.

1851



(b)

- 1854
- 1855

1857

1858

1859 Progressive Updating of the Diagram When Hypotheses Are Successfully Rejected 1860

1861 The graphical approach guides the hierarchical testing of multiple hypotheses through continual 1862 updating of the initial graph whenever a hypothesis is successfully rejected. The initial graph 1863 represents the full testing strategy (with all hypotheses). Each new graph shows the progression 1864 of the testing strategy by eliminating hypotheses that have been rejected and retaining those yet 1865 to be tested or re-tested.

1866

1867 When there is a desire to consider analysis strategies with complex division of alpha, the 1868 graphical method and progressive updating of the diagram can aid in understanding the

- 1869 implication of the different strategies for a variety of different hypothetical scenarios. This
- 1870 progressive updating can aid in selecting which specific strategy to select for the final study

1871 statistical analysis plan.

1872

Figure A5 is an example of how the graphical method aids in formulating the testing of three hypotheses H_1 , H_2 , and H_3 and illustrates the updating of the diagram when a test of hypothesis is

¹⁸⁵⁶ **Figure A4:** Fallback (a) and improved fallback (b) procedures.

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1875 successful. For this example, the analysis plan designated two hypotheses, H_1 and H_2 , to be of 1876 prime importance (i.e., primary endpoints), and H_3 (the secondary endpoint) is tested only if the test results for H_1 and H_2 are both significant. Assume that it is desired to always be able to test 1877 both H_1 and H_2 (i.e., a willingness to split the available alpha between them), but that if either H_1 1878 1879 or H_2 is successfully rejected, the alpha level of that test would be passed to the other hypothesis 1880 if needed, so that it can be tested at the maximal possible alpha level (i.e., the fallback method is 1881 specified for the two important endpoints, with α_1 assigned to begin testing on H₁, and α_2 1882 reserved as the minimum that will be available for testing H_2). Thus, as shown in Figure A5 (a), 1883 if the test result for H₁ is significant, then its endpoint-specific alpha level α_1 is passed to H₂, so 1884 that H₂ is tested at an endpoint-specific alpha level of $\alpha_1 + \alpha_2 = \alpha$. On the other hand, if the test 1885 result for H_1 is not significant, H_2 is still tested with the reserved α_2 . In this case, however, if the 1886 test result for H₂ is significant, the alpha level of α_2 is recycled back to re-testing of H₁ at level α_1 $+\alpha_2 = \alpha$. Note that the graphical method aids in communicating that the re-testing of H₁ at an 1887 1888 increased endpoint-specific alpha is part of the prospective analytic plan.

1889

1890 The intended analysis, however, is that if, and only if, these tests of hypotheses (including

1891 potential re-test with passed alpha) have successfully rejected H_1 and H_2 , then the full available

alpha would be passed to H₃. This conditional passing of alpha is depicted by a path from H₂ to H₃ with weight ε . At the start (before any testing of any hypothesis) ε is set to a negligible amount. Because of this, even though there is a path from H₂ to H₃, when H₁ has not yet been successfully rejected, essentially all of α_2 will be passed back to H₁ as the priority over H₃. This scheme will eventually allow for meaningful testing of H₃ if appropriate according to the sequentially updated diagrams.

1898

1899 Figure A5 (b) shows the updated graph when the result for H_1 in Figure A5 (a) is significant at 1900 level α_1 and prior to testing H₂ at the now accumulated endpoint-specific alpha of $\alpha_1 + \alpha_2$ (which 1901 would be equal to the total alpha for the study in this case). Note that the weight on the path 1902 from H_2 to H_3 is now set to 1. This occurs because diagram updating is done when a test of 1903 hypothesis is significant. The process of diagram updating first passes along the retained alpha 1904 from the successful hypothesis (vertex) according to the weights on the arrows leaving that 1905 vertex. That vertex is then eliminated from the diagram and a new diagram is constructed by 1906 connecting all the incoming paths (arrows) to all outgoing paths (tails) of the now deleted vertex, 1907 and adjusting the pathway weights. The new weights on the new paths are determined based on 1908 the relative weights of each previous part of the new path. The essential principle of 1909 readjustment of the pathway weights is that the sum of the weights on the outgoing paths from 1910 each vertex must be 1.0. This rule causes the weight on the path from H_2 to H_3 to become 1 1911 (from the prior negligible fraction ε) because it is the only remaining path leaving H₂. In some 1912 strategies, a newly created connection path arising from elimination of a successful vertex will 1913 duplicate a preexisting direct connection between two vertices; in this case the weights of the 1914 duplicate paths are combined and drawn as a single path.

1915

1916 Continuing with the example depicted in Figure A5, if H_1 is not initially significant and H_2 is

1917 significant at level α_2 , Figure A5 (c) shows the updated diagram prior to re-testing H₁ at the now

1918 accumulated endpoint-specific alpha. The vertex for H₂ was eliminated from the updated

1919 diagram, and the direct path from H_1 to H_3 is displayed. Both Figures A5 (b) and A5 (c) indicate

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1920 that H₃ can be tested at the full level α (= $\alpha_1 + \alpha_2 + 0$) when the test results for H₁ and H₂ are both 1921 significant, but that no alpha is passed to H₃ unless both H₁ and H₂ were significant.



(c)

1922

Figure A5: Graphical illustration of the fallback procedure applied to three hypotheses when the first two hypotheses are most important and the third hypothesis is tested only when both of the first two hypotheses are significant.

- 1926(a) The initial diagram shows all hypotheses and paths. The notation ε indicates a positive1927number close to zero. This convention indicates the potential to pass alpha to H₃, but only1928if it is not necessary to pass alpha from H₂ to H₁ (see text for explanation).
 - (b) The updated diagram shows the case where only H_1 was tested and shown to be statistically significant.
- 1931 (c) The updated diagram shows the case where H_2 was the first hypothesis to be statistically 1932 significant at the initially allocated endpoint-specific alpha.
- 1933

- A detailed algorithm for iteratively updating the graph when a test is found significant is
- 1935 illustrated with the final example. Updating of a graph involves determining new endpoint-
- 1936 specific alpha levels and path weights based on satisfying the conditions that (1) the sum of all
- 1937 endpoint-specific alpha levels equals α and (2) the sum of all weights on outgoing arrows from a
- 1938 vertex to others equals 1.0.
- 1939

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1940 1041	The case of three hypotheses with fixed weights on the paths between the hypotheses will be used to illustrate the algorithm (Figure $\Delta f_{(a)}$). Suppose that hypothesis H _a is rejected. The
1941	used to infustrate the algorithm (Figure Ao (a)). Suppose that hypothesis 113 is rejected. The
1942	graph needs to be updated to remove this hypothesis and retain hypotheses H_1 and H_2 .
1943	Calculations for this are as follows:
1944	
1945	1. New alpha level at $H_1 = \text{old alpha level at } H_1 + w_{31} \times (\text{the alpha level at } H_3) = \alpha/3 + (1) \times (1)$
1946	$(\alpha/3) = 2\alpha/3$. (The weight w ₃₁ is for the arrow going from H ₃ to H ₁ .)
1947	2. New alpha level at H ₂ = old alpha level at H ₂ + w ₃₂ × (the alpha level at H ₃) = $\alpha/3$ + (0) ×
1948	$(\alpha/3) = \alpha/3$. (Note that there is no arrow shown from H ₃ to H ₂ , as its weight w ₃₂ = 0.)
1949	3. New weight w_{12} for the arrow going from H_1 to $H_2 = (old w_{12} + A)/(1 - B)$, where
1950	A = additional weight for H ₁ to H ₂ going through H ₃ = $w_{13} \times w_{32} = (1/3) \times (0) = 0$, and
1951	\mathbf{B} = adjustment for the arrow going from \mathbf{H}_1 to \mathbf{H}_3 and returning back to $\mathbf{H}_1 = \mathbf{w}_{13} \times \mathbf{w}_{31} =$
1952	$(1/3) \times (1) = 1/3$. Therefore, new $w_{12} = (2/3 + 0)/(1 - 1/3) = 1$.
1953	4. Similarly, new weight w_{21} for the arrow going from H_2 to $H_1 = (old w_{21} + w_{23} \times w_{31})/(1 - w_{23} \times w_{31})/(1 $
1954	$(\times w_{32}) = [1/2 + (1/2) \times (1)]/[1 - (1/2) \times (0)] = 1.$
1955	
1956	This gives the updated graph in Figure A6 (b). Similar calculations can be made for graphs for
1957	H_1 and H_3 if H_2 is rejected and for H_2 and H_3 on rejecting H_1 .



1959 1960 Figure A6: Initial diagram (a) for three hypotheses with fixed weights on the paths connecting the hypotheses, and updated graph (b) when hypotheses H_1 and H_2 are not yet rejected but H_3 is 1961 rejected. 1962

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